CAS CS 131 - Combinatorial Structures Spring 2011

PROBLEM SET #7 (COUNTING) OUT: FRIDAY, APRIL 6 DUE: FRIDAY, APRIL 13

NO LATE SUBMISSIONS WILL BE ACCEPTED

To be completed individually.

- Next week, I'm going to get really fit! On day 1, I'll exercise for 10 minutes. On each subsequent day, I'll exercise 5, 6, 7 or 8 minutes more than the previous day. For example, the number of minutes that I exercise on the second day of next week might be 15, 16, 71, 18. How many such sequences are possible (within a week)?
- 2. From a group of 10 men, 5 women, 4 boys, and 6 girls,
 - (a) In how many ways can a man, a woman, a boy, and a girl be selected?
 - (b) In how many ways can one person, that is either a man or a girl, be selected?
 - (c) In how many ways can one person be selected?
- 3. How many ways are there to distribute seven different books among twelve people if no person is to receive more than one book?
- 4. Find an appropriate bijective mapping between a set of sequences and the set in question:
 - In how many ways can k elements be chosen from an n-element set $\{x_1, x_2, \dots, x_n\}$?
 - How many different ways are there to select a dozen donuts if five varieties are available?
 - How many different solutions over the natural numbers are there to the equation: $x_1 + x_2 + x_3 + \cdots + x_8 = 90$? A solution is a specification of the value of each variable x_i . Two solutions are different if different values are specified for some variable x_i .
 - An electronic toy displays a 3×3 grid of colored squares. At all times, three are red, three are green, and three are yellow. How many such configurations are possible?
- 5. How many *even* numbers in the range 1000–9999 have no repeated digits?
- 6. In a 12-day period, a small business mailed 196 bills to customers. Show that during some period of four consecutive days at least 66 bills were mailed.