

# Social Influence and the Diffusion of User-Created Content

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# Motivation

- Direct transfers between users
- More precise identification of heavy influencers
- Simple model of adoption rates
- Importance of network effects

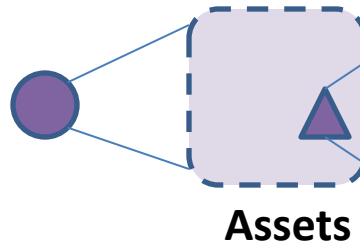




# Data Set

- content ownership data (3,409,630 entries)
  - name of content
  - previous owner
  - next owner
  - time stamp
- weekly snapshots of the social graph from Sept. 2008 to Jan. 2009
- user data
  - date joined
  - number of hours played

# Definitions



## Active user

- last login after Nov 2008
- play time > 60 hours
- exchanged at least 1 item with another user

## Gesture

- at least 16 unique owners
- user-created only

## Sample

- 100,229 users
- 106,499 assets

# Observations and Further Definitions

48% of transfers occurred between friends  
users share assets within short time of receiving

For each asset:

**Asset size:** total number of adopters

**% direct:** percentage of transfers  
between friends

**% non-leaf:** percentage of non-terminating  
transfers

**social influence:** a friend adopts before you do

**direct influence:** obtaining an asset from a friend

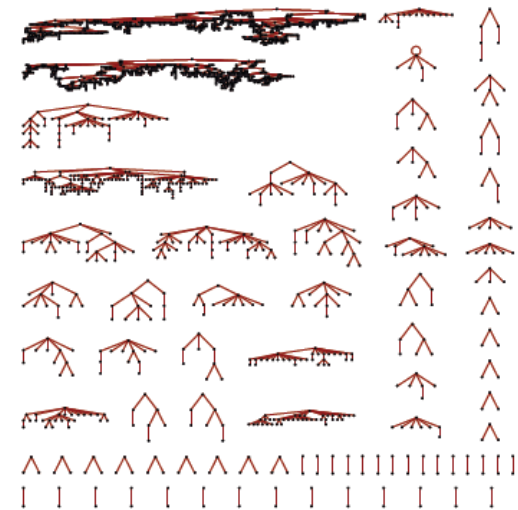
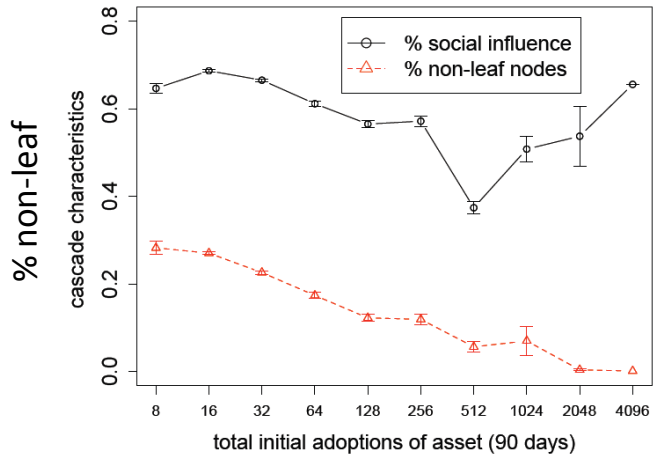


Figure 2: Example of a cascade forest for the Aero-smith(916) gesture. Edges denote transfers of the gesture between users.

# Regression



- **asset size or popularity:** total number of adopters
- **% social:** adoptions occurred after at least one friend adopted
- **% non-leaf:** percentage of non-terminating transfers

↑ % social

↓ number of additional adoptions

speed of individual transfers ↑ between friends

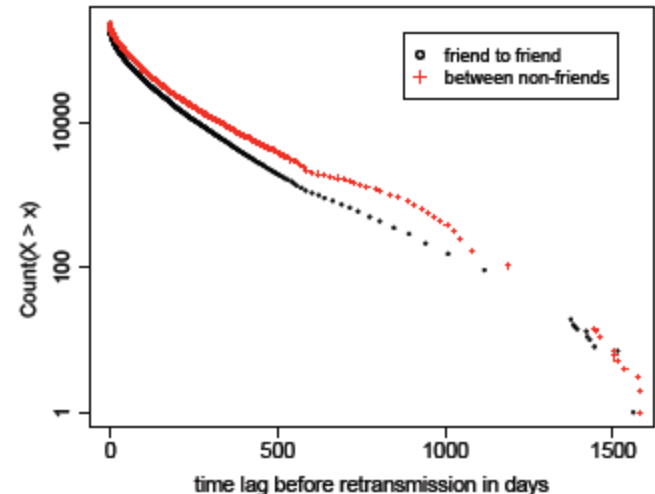
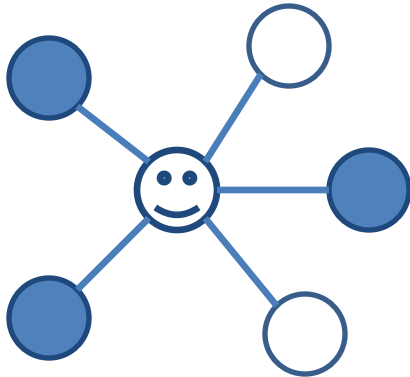


Figure 4: Delays between a users' adoption and retransmission times, for assets with 100-200 adopters.

# Rate of Adoption for an Asset



state  $k$

$k$  friends have adopted the asset

$T_k$  exp dist. w/ mean  $\frac{1}{\lambda_k}$   
 ↑  
 Time until adoption  
 ←  
 Rate of adoption for state  $k$

$$M_k = \sum_i t_k^i \quad \text{Total time spent in state } k \text{ over all users } i$$

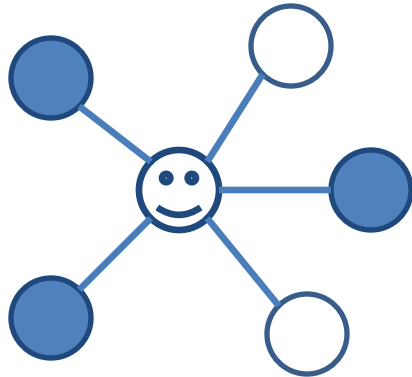
$A_k$  Number of users who adopted at state  $k$

$$\lambda_k = \frac{A_k}{M_k}$$

Probability Density  $F(k)$

$$\prod_k \lambda_k^{A_k} e^{-\lambda_k M_k}$$

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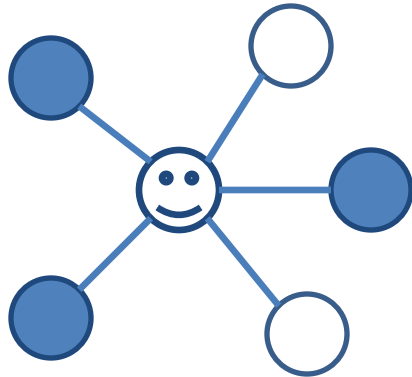
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Probability Density  $F(k)$

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# Rate of Adoption for a User



state  $k$

$k$  friends have an asset  $i$

$T_k$  exp dist. w/ mean  $\frac{1}{\lambda_k}$   
 ↑  
 Time until adoption  
 Rate of adoption for state  $k$

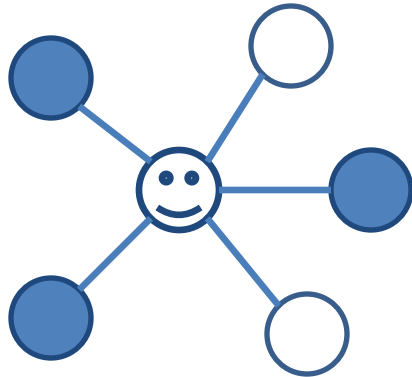
$$M_k = \sum_i t_k^i \quad \text{Total time the user spent in state } k \text{ for the asset } i$$

$A_k$  Number of assets adopted from state  $k$

$$\lambda_k = \frac{A_k}{M_k}$$

Simplified Probability Density  $\prod_k \lambda_k^{A_k} e^{-\lambda_k M_k}$

# Rate of Adoption for a User



state  $k$

$k$  friends have an asset  $i$

$T_k$  exp dist. w/ mean

$$\frac{1}{\lambda_k}$$

Time until adoption

Rate of adoption for state  $k$

$$M_k = \sum_i t_k^i$$

Total time the user spent in state  $k$   
over all assets the user was observed to adopt

$A_k$  Number of assets adopted from state  $k$

$$\lambda_k = \frac{A_k}{M_k}$$

Simplified Probability Density  $\prod_k \lambda_k^{A_k} e^{-\lambda_k M_k}$

# Submodularity

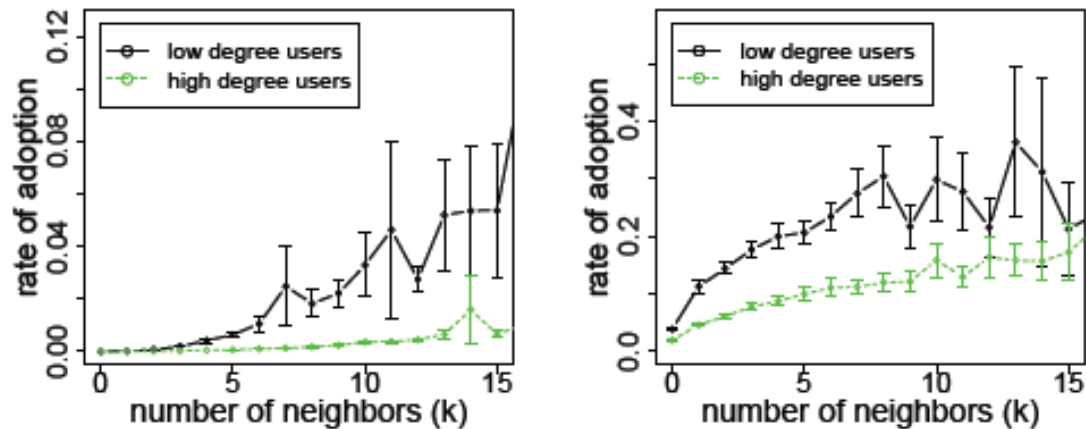


Figure 6: The average rate of adoption for users as function of adopting neighbors,  $k$ . The black curve corresponds to users of low degree that have 15-100 friends, and the green curve corresponds to users with 100-1000 friends. Left: entire population of assets. Right: adopted population of assets. The rates are in units of inverse days.

# Comparison with Cox Model of Adoption

↑ # adopting friends

↑ chance of own adoption

↑ average degree

↓ adoption rate

↑ total # of adopters

↑↓ adoption rate

↑ user experience (time)

↓ adoption rate of friends' content

# Influence

## Measuring Entropy of Users Responsible for Transfers

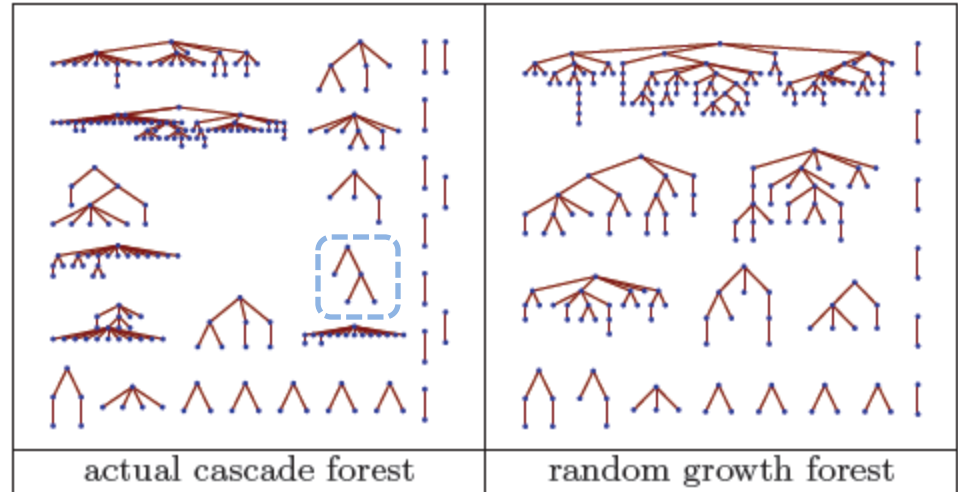
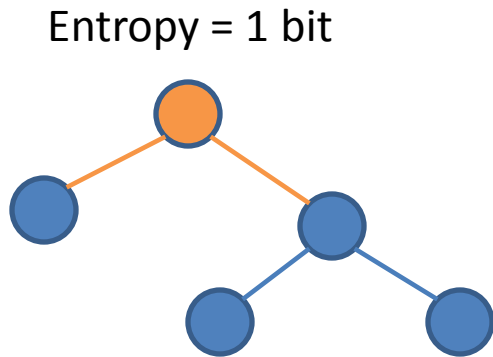


Figure 8: Comparison between actual growth of cascades and a null model where each previous adopter is equally likely to be sharing assets.

Our Model:  
2.72 bits

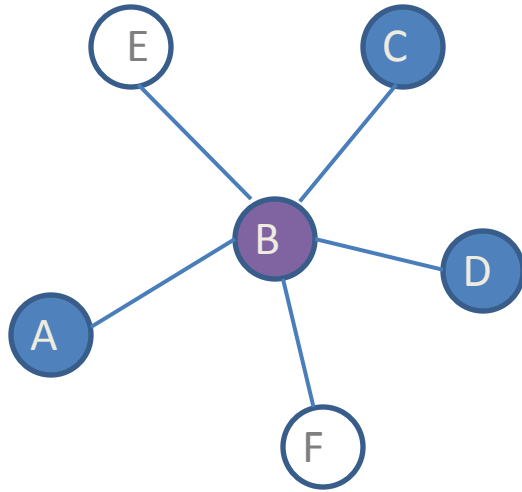
Null Model:  
3.48 bits

Proportion of missing edges in the cascade

$$Null\ Model(n, p)$$

Total number of owners of the asset

# Strength of Influence



Transfers : # of A to B transfers

Expected:  $E[\text{A to B transfers}]$   
 $+ \text{Pr}[\text{A was the one who transferred asset to B}]$

$$\gamma = \frac{\text{transfers} - \text{expected}}{\text{expected}}$$

Mean: -0.286

↑ number of friends

↓  $\gamma$  score

↑ number of assets

↓  $\gamma$  score

↑ number of transfers to friends / assets owned

↑  $\gamma$  score

— Earlier asset acquisition

—  $\gamma$  score

# Early Adopters vs. Later Adopters

$\geq 20$  gestures or  $\geq 40$  gestures  
Among first 5% or 10 % of adopters for all  
owned assets



$\geq 20$  gestures  
Latter half of adopters

68 days earlier  Joined Second Life

 time spent playing 

8  number of friends

-0.08      Gamma scores      -0.22

 number of transfers 

 Future popularity of assets adopted

 Pr[you adopt before your friends]

 Gamma score

 number of transfers

# Conclusions

↑ rate of adoption

↑ friends adopt

↓ asset popularity

↑ friends

↓ likely to be influenced by any one of them

↑ friends

↓ one's own direct influence

↑ strength of friendship

↑ number of assets transferred

early adopters have **no** greater influence



# Additional Equations

Probability Density

$$\prod_i \lambda_{a_i}^{\theta_i} e^{-\sum_k \lambda_k t_k^i}$$

Over all users/assets  $i$

State from which the user adopted the asset  
(if the user did adopt)

Total time  $i^{\text{th}}$  user/asset spent in state  $k$

1 if user adopted by end of observation period  
0 otherwise