## CS 235: Algebraic Algorithms, Spring 2021

## Discussion 6

Tuesday, March  $30^{th}$ , 2021.

## **Problem 1.** Cosets and Quotient Groups:

- (a) Find all cosets of subgroup  $\langle 4 \rangle$  of  $\mathbb{Z}_{12}$ .
- (b) Find the index of the quotient group  $\mathbb{Z}_{24}/\langle 3 \rangle$ . What are its elements?

**Problem 2.** Group Isomorphism: explain why the following pairs of groups are (or are not) isomorphic.

- (a)  $\mathbb{Z}_4$  and  $\mathbb{Z}$
- (b)  $\mathbb{Z}_2 \times \mathbb{Z}_2$  and  $\mathbb{Z}_4$
- (c)  $\mathbb{Z}_8^*$  and  $\mathbb{Z}_{12}^*$

**Problem 3.** Exponent of a Group: find the exponent of the following groups.

- (a)  $\mathbb{Z}_{35}$  and  $\mathbb{Z}_{15} \times \mathbb{Z}_{35}$
- (b)  $\mathbb{Z}_{15}^*$  and  $\mathbb{Z}_{600}^*$ .