

## Homework 12 – Due Thursday, December 8, 2016 on Canvas

Please refer to HW guidelines from HW1, course syllabus, and collaboration policy.

**Exercises** These should not be handed in, but the material they cover may appear on exams:

1. Chapter 8, problem 1.
2. Chapter 8, problem 2.
3. (**Multiple Interval Scheduling**) Chapter 8, problem 14.
4. (**Cycle Cover**) Chapter 8, problem 41(b).

### Problems to be handed in

1. (**Carpenter's Ruler**) Consider the decision version of the Carpenter's Ruler problem from homework 6.

Given a carpenter's ruler consisting of  $n$  line segments of integer length  $\ell_1, \ell_2, \dots, \ell_n$ , decide whether it can be folded into length at most  $k$ .

Prove that this problem is NP-complete. To prove NP-hardness, reduce from NUMBER PARTITIONING PROBLEM defined as follows:

Given a set of  $n$  positive integers  $x_1, \dots, x_n$ , decide whether the numbers can be partitioned into two sets  $S_1$  and  $S_2$  with the same sum:

$$\sum_{x_i \in S_1} x_i = \sum_{x_i \in S_2} x_i.$$

2. (**Independent Set on a Grid**) KT, Chapter 11, Problem 10.