

**Problem** Linking track fragments with short-term, long-term or multi-view occlusions

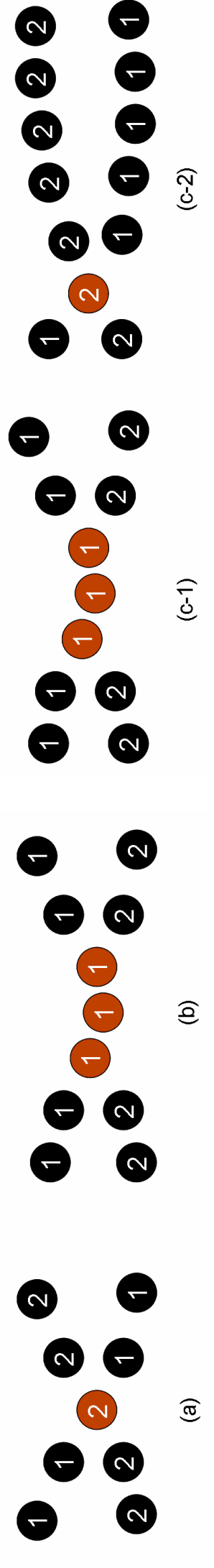


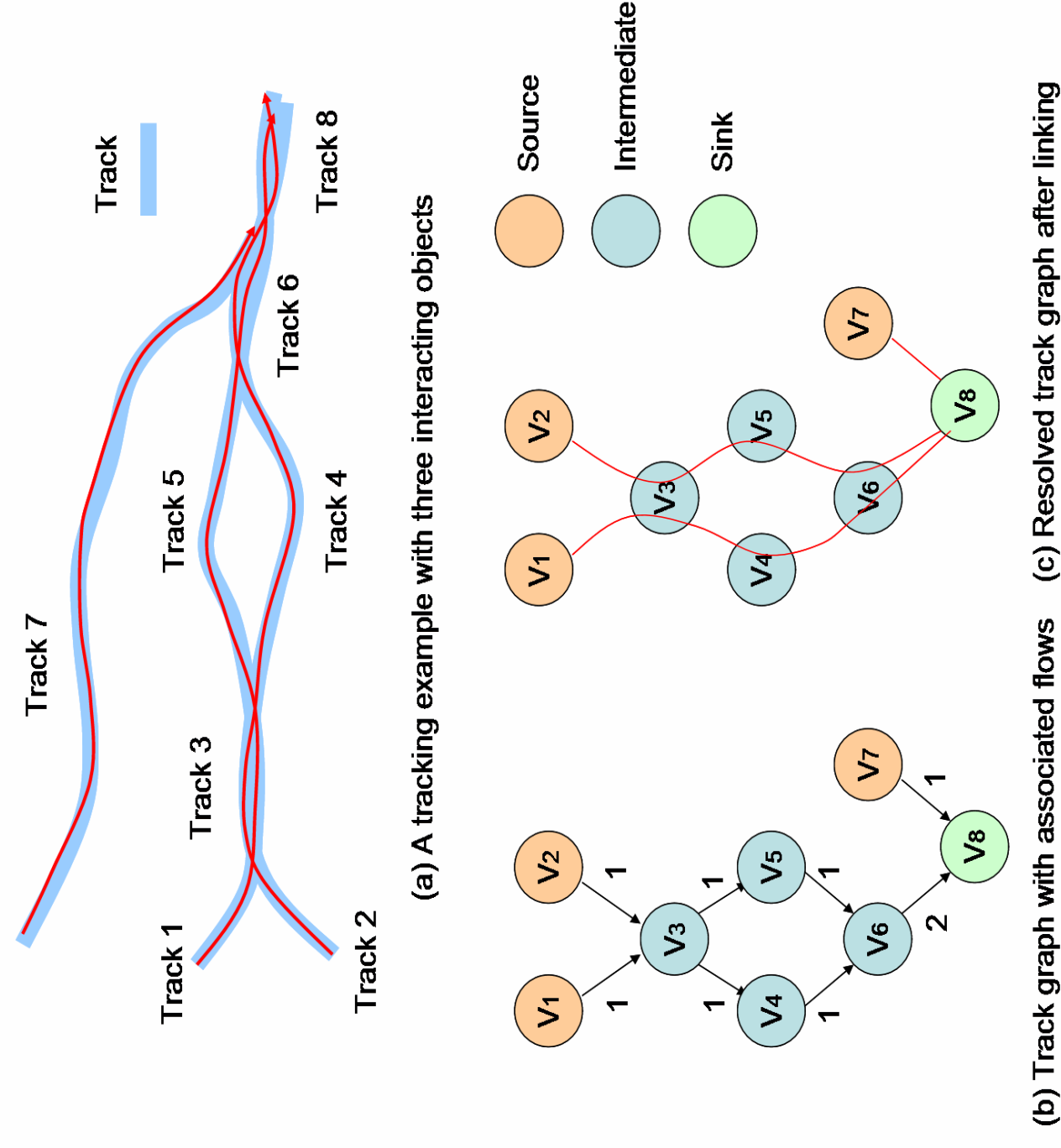
Fig. 1 (a) Short-term occlusion, (b) Long-term occlusion, and (c) Occlusion in two camera views. Red nodes represent merged measurements; numbers are labels for objects.

**Contributions**

- For short-term occlusion, our method automatically constructs the track graph and resolves it by computing the minimum flow and a series of bipartite graph matches.
- For long-term occlusion, we convert the problem of track graph reasoning to the standard set cover problem, for which a logarithmic approximation solution exists.
- For occlusions in multiple views, our method constructs the track graph for each view independently and resolves the track graphs jointly by solving a joint-set-cover problem. To the best of our knowledge, we are the first to formulate the track linking problem in both the temporal (across-time) and spatial (across-camera) domains.

**Track Graph**

Define track graph  $G=(V,E)$ , where  $V$  is set of vertices that represent individual or merged tracks.  $E$  is set of directed edges that represent merging or splitting events.  $f$  is the flow on the edge indicates how many objects are involved during the merging or splitting event.  $t_v$  is the track capacity that shows how many objects the track contains.



**Track Graph Construction**

- Building the structure of graph: tracking forward and backward to produce the tracklets and merge/split hypothesis. For example, if multiple trackers predict a collision in image in next frame, all trackers are terminated and a new tracker is initiated to track the overlapped measurements.
- Determine the flow: solving a minimum-flow problem where the lower bound on the capacity of each edge is one. False alarm tracklets are assumed to be identified and excluded during the building stage.

**Local Linking Method**

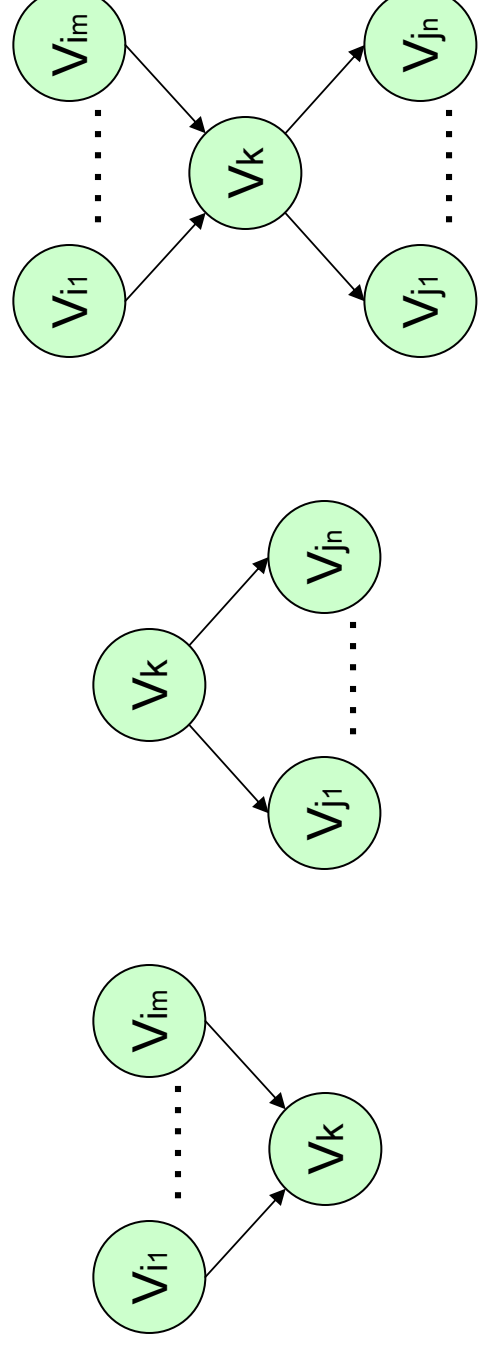


Fig. 2 The local structure of track graph can only have three types shown above. Only the last type needs a nontrivial reasoning which is a bipartite matching problem.

**Global Linking Method**

A generalized set-cover formulation:

For a given track graph, we enumerate all possible paths from source set  $S$  to sink set  $T$ , where each path consists of a sequence  $\{V_{p1}, V_{p2}, \dots, V_{pd}\}$  of vertices visited. The set of all paths is denoted as  $P$ . A weight  $w_p$  is associated with a path  $p$  that measures the likelihood of the path being a true trajectory, or equivalently the cost of the path. The objective is to select a subset  $P'$  of  $P$  such that the sum of the costs of all selected paths is minimum. Each vertex  $v$  from  $G$  has to be in some path at least  $t_v$  times, where  $t_v$  is the track-capacity of  $v$  computed from the minimum flow during the construction of the graph.

Solver: Greedy Method or Linear Relaxation (same approximation quality)

**Linking in Multiple Views**

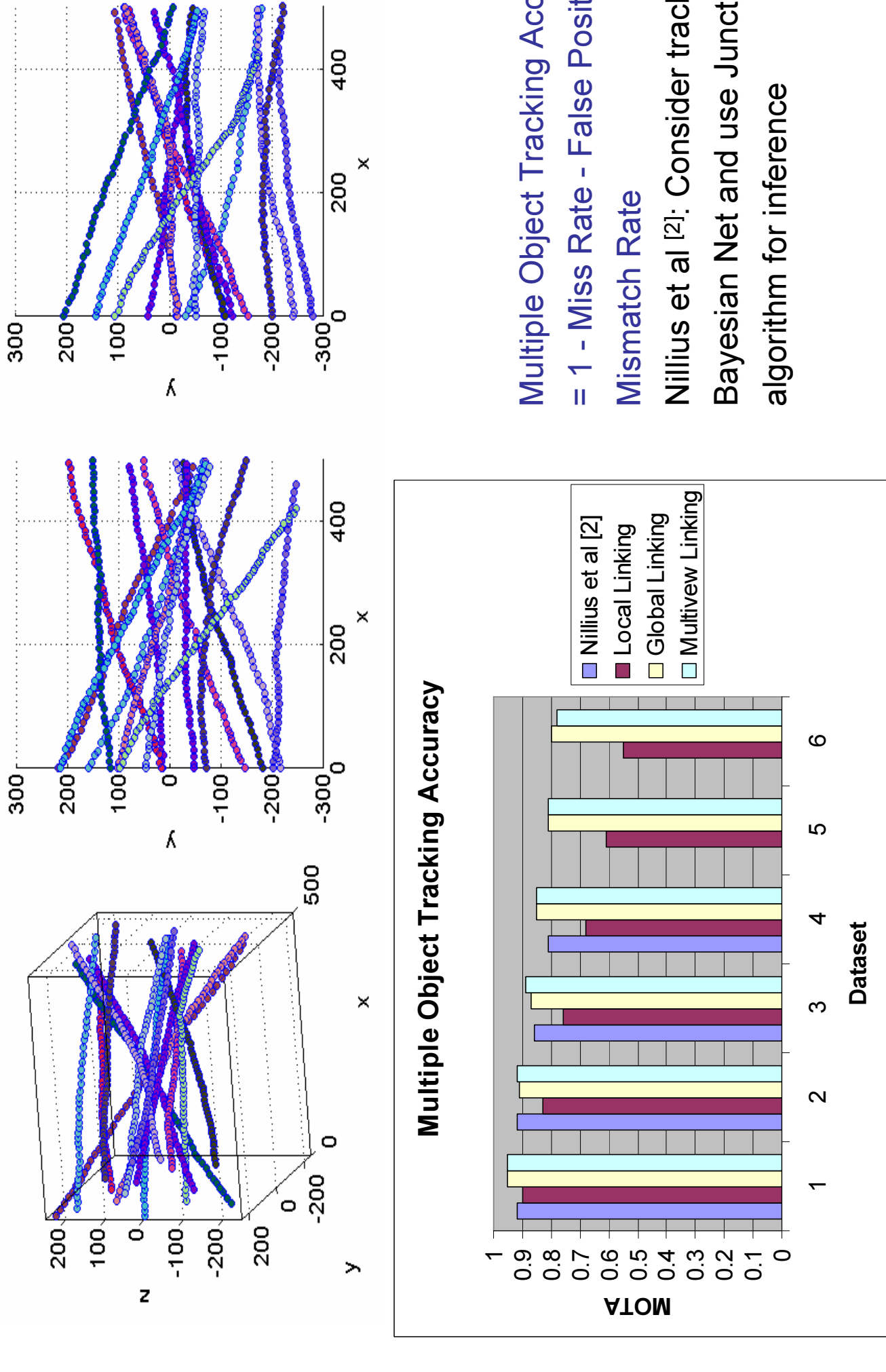
A joint set-cover formulation:

Given two track graphs  $G_1 = (V_1, E_1)$  and  $G_2 = (V_2, E_2)$ , enumerate all valid paths as set  $P_i$ . Compute  $a_p$  and  $b_q$  to measure the respective likelihood of path  $p$  in  $P_1$  and  $q$  in  $P_2$  being true trajectories. The objective is to choose a subset  $P'_i$  to achieve a cover on  $V_i$  for each view, subject to the additional constraint that enforces that any selected path  $p$  in  $P'_i$  has a corresponding path  $q$  in  $P'_j$  with matching cost  $c_{p,q}$ . We seek the solution that achieves the minimum weighted sum.

**Proposition:** The joint set-cover problem can be reduced to a standard set cover problem

**Experiment 1: Synthetic Data**

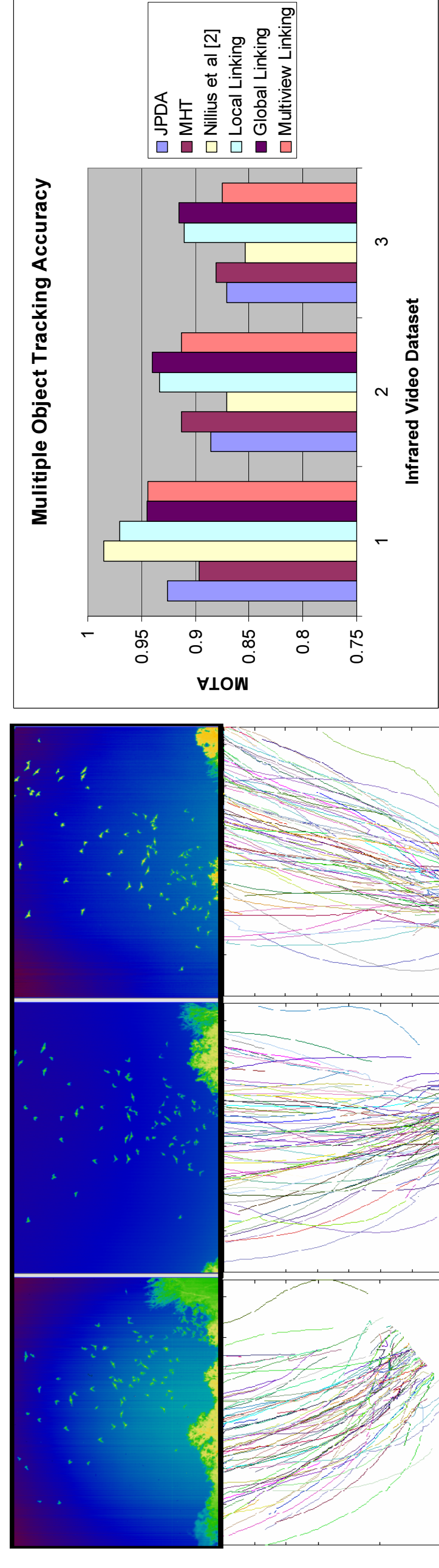
Randomly generated spheres using a linear dynamic model with constant velocity plus Gaussian noise. 6 datasets of increasing density (up to 60 objects per frame) with two views were tested.



Multiple Object Tracking Accuracy (MOTA)<sup>[1]</sup>  
 = 1 - Miss Rate - False Positive Rate - Mismatch Rate  
 Nililius et al [2]: Consider track graph as Bayesian Net and use Junction-Tree algorithm for inference

**Experiment 2: Infrared Thermal Video Analysis**

3 Datasets of increasing density (up to 100 objects per frame) with three thermal infrared cameras.



[1] K. Bernardin and R. Stiefelhagen. Evaluation multiple object tracking performance: The CLEAR MOT metrics. EURASIP Journal on Image and Video Processing, 2008  
 [2] P. Nililius, J. Sullivan, and S. Carlsson. Multi-target tracking: Linking identities using Bayesian network inference. In CVPR, 2006.