



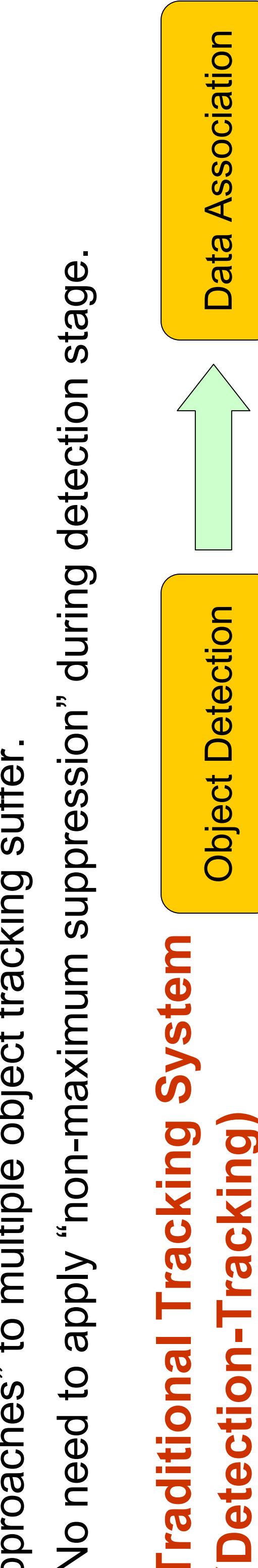
Coupling Detection and Data Association for Multiple Object Tracking

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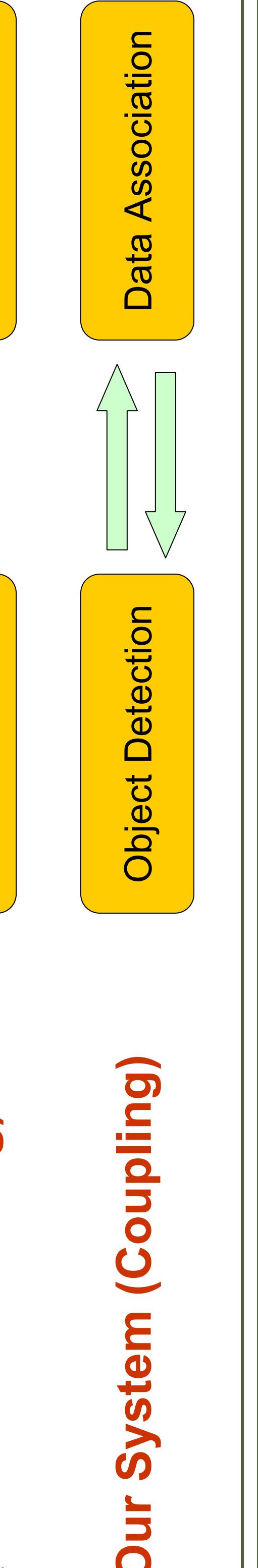
Abstract

We present a novel framework for multiple object tracking in which the problems of object detection and data association are expressed by a **single** objective function. The framework follows the Lagrange dual decomposition strategy, taking advantage of the often complementary nature of the two subproblems. The advantages of our coupling framework are:

- No problem of error propagation from which traditional “detection-tracking approaches” to multiple object tracking suffer.
- No need to apply “non-maximum suppression” during detection stage.



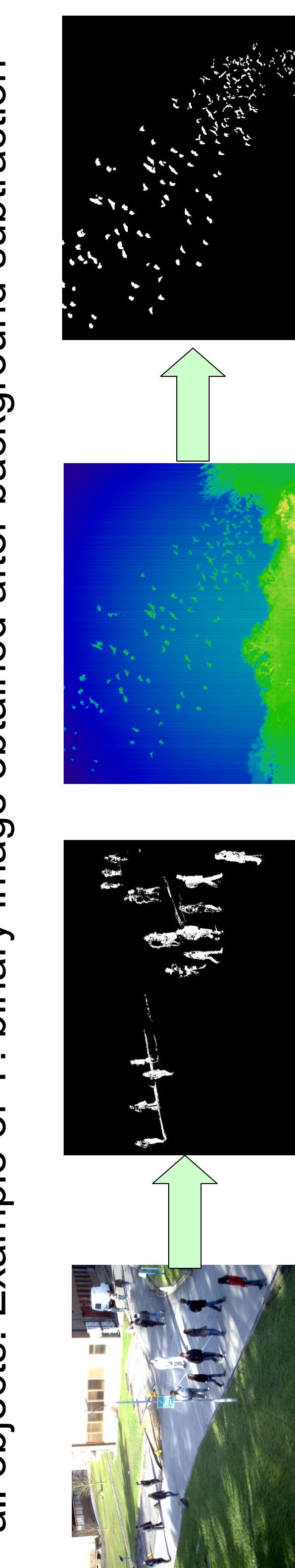
Our System (Coupling)



Bayesian Formulation

$$\begin{aligned} \max_X p(X | Y) &= \max_X p(Y | X)p(X) \\ &= \max_X \prod_t p(Y_t | X_t) \prod_t p(X_t | X_{t-1}) \\ &\approx \max_X \prod_t p(Y_t | X_t) \prod_i p(x_{i,t}) \prod_t p(x_{i,t} | X_{t-1}) \end{aligned}$$

X is the joint state vector of **all** objects in the scene
 Y is the observation vector for the **entire** image, which depends on the states of all objects. Example of Y : binary image obtained after background subtraction



General Form of the Objective Function

$$\begin{aligned} \max_X p(X | Y) &\rightarrow \min_{X_1, X_2} g(X_1, Y) + h(X_2) \\ \text{s.t. } X_1 &= q(X_2) \end{aligned}$$

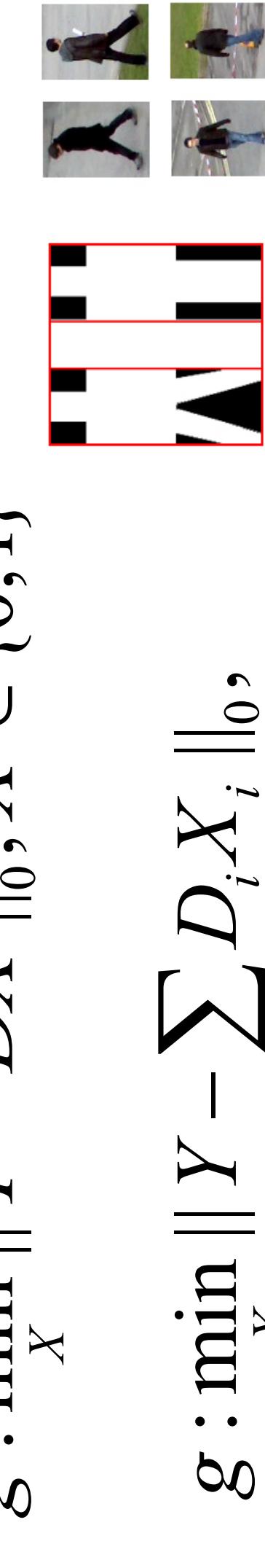
- Function $g(\cdot)$ can be seen as the objective function in detection problem (image likelihood term); $h(\cdot)$ is the objective function in data association problem (temporal smoothness term); $q(\cdot)$ is the coupling constraint to enforce **agreement** of the solutions between two sub-problems.
- The choices of g , h , q and their combination are flexible. Typically, we want g , h are relatively easy to optimize.
- For traditional detection-tracking scheme with independence likelihood assumption ($h(\cdot)$ does not model the joint image likelihood), there is no need to introduce coupling constraint; the objective function is equivalent to classic tracker such as Multiple-Hypothesis-Tracking or Network-Flow-Tracker.
- The overall optimization can be solved through **Dual Decomposition**

Sparsity-constrained Detection

Given a **dictionary** D that encodes the shape and spatial information of objects in image, instantiate **binary templates** at selected positions through **selector** X such that the generated image (DX) looks similar to the observation Y .

Single Template

$$g : \min_X \|Y - DX\|_0, X \in \{0,1\}^N$$



Multiple Templates

$$g : \min_X \|Y - DX\|_0, X \in \{0,1\}^N$$

$$\text{s.t. } \sum_i X_{i,n} \leq 1, X_i \in \{0,1\}^N$$

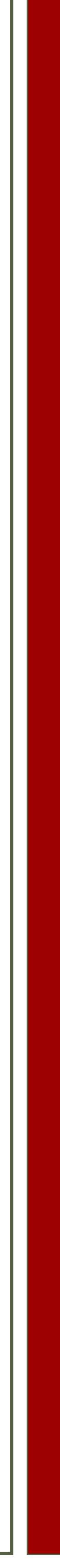
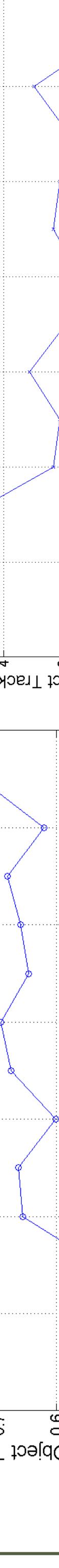
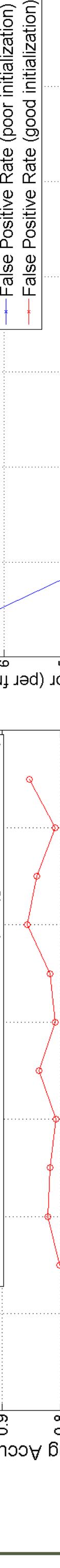
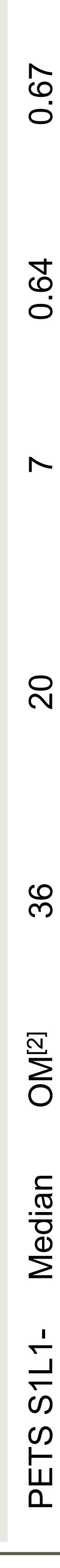
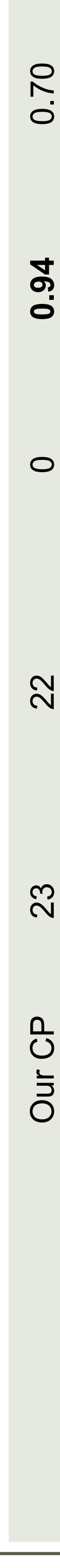
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Localization in 2D (Ground Plane)



Experiment



Coupling Detection and Data Association

$$\begin{aligned} \min_{X,f} \sum_t \|Y_t - D_t X_t\|_0 + \sum_t \sum_i \sum_j c_{i,j}^{(t)} f_{i,j}^{(t)} \end{aligned}$$

Dual Decomposition

$$\begin{aligned} \text{s.t. } \sum_i f_{i,n}^{(t)} &= \sum_j f_{n,j}^{(t)}, \\ X_{t,n} &= \sum_j f_{n,j}^{(t)}, \quad \forall t \forall n \end{aligned}$$

Flow conservation: If there is a flow coming into a node, there is a flow going out.

Variable agreement: If there is a detection at a node, there is a flow going through.

$$h(\lambda) = \min_f \sum_j (\|Y_t - D_t X_t\|_0 + \lambda^T X_t) \quad h(\lambda) = \min_f \sum_j (\sum_i c_{i,j}^{(t)} - \lambda_i) f_{i,j}^{(t)}$$

Experiment

