



TEL AVIV UNIVERSITY

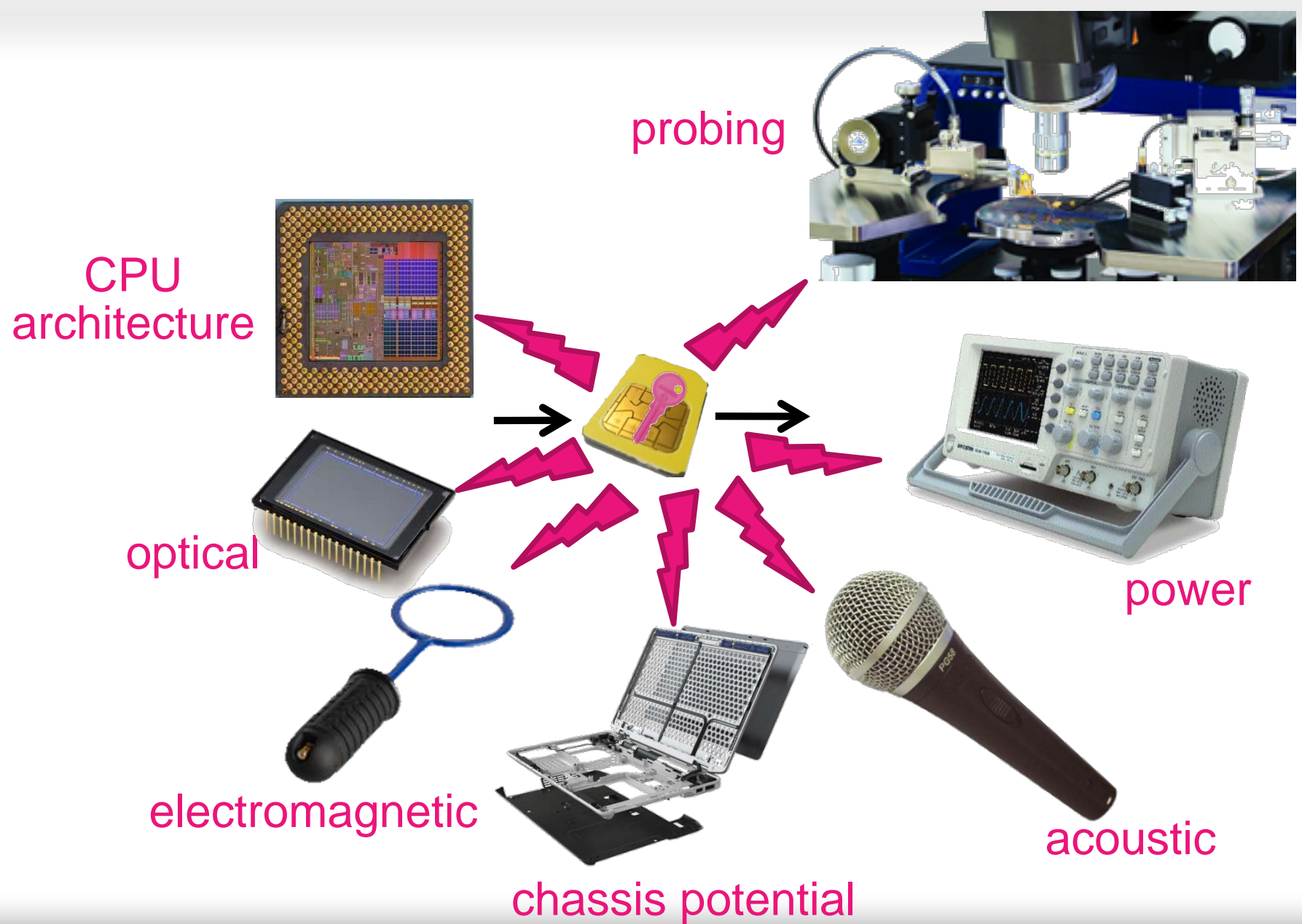
# Information Security – Theory vs. Reality

0368-4474, Winter 2015-2016

## **Lecture 6: Physical Side Channel Attacks on PCs**

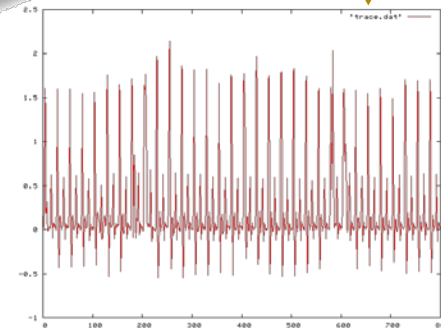
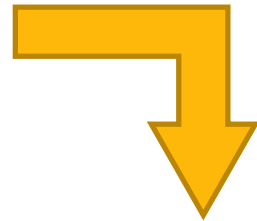
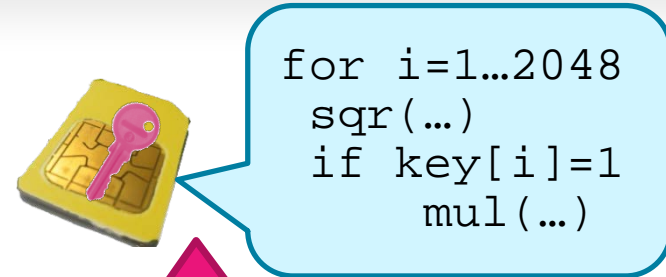
Guest lecturer:  
Lev Pachmanov

# Side channel attacks



# Traditional side channel attacks methodology

1. Grab/borrow/steal device
2. Find key-dependent instruction
3. Record emanations using high-bandwidth equipment (> clock rate , PC: >2GHz)
4. Obtain traces
5. Signal and cryptanalytic analysis
6. Recover key



Hard for PCs



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Not handed out



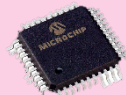
vs.



Complex electronics running complicated software (in parallel)



vs.



Measuring a 2GHz PC requires expansive and bulky equipment (compared to a 100 MHz smart card)



vs.



1,000\$

100,000\$

# Our results

- Channels for attacking PCs

- Ground potential (chassis and others)
- Power
- Electromagnetic
- Acoustic



- Exploited via low-bandwidth cryptanalytic attacks

- Adaptive attack (50 kHz bandwidth) [Genkin Shamir Tromer '14]
- Non-adaptive attacks (1.5 MHz bandwidth)  
[Genkin Pipman Tromer '14] [Genkin Pachmanov Pipman Tromer '15]



- Common cryptographic software

- GnuPG 1.4.13-1.4.16 (CVE 2013-4576, 2014-3591, 2014-5270)
- RSA and ElGamal, various implementations
- Worked with GnuPG developers to mitigate the attacks



- Applicable to various laptop models



**Chassis-potential channel**

# Ground-potential analysis

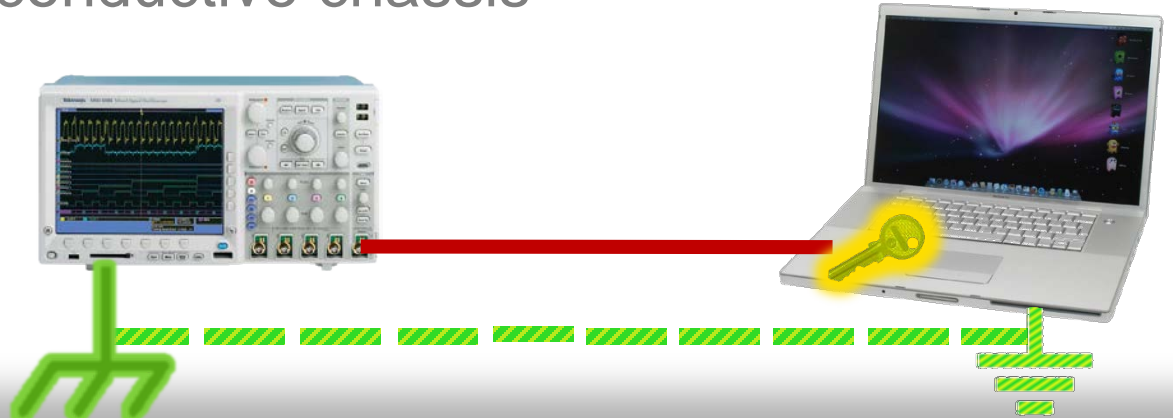
- **Attenuating EMI emanations**  
“Unwanted currents or electromagnetic fields?  
Dump them to the circuit ground!”  
(Bypass capacitors, RF shields, ...)
- Device is grounded, but its “ground” potential fluctuates relative to the mains earth ground.



## Computation

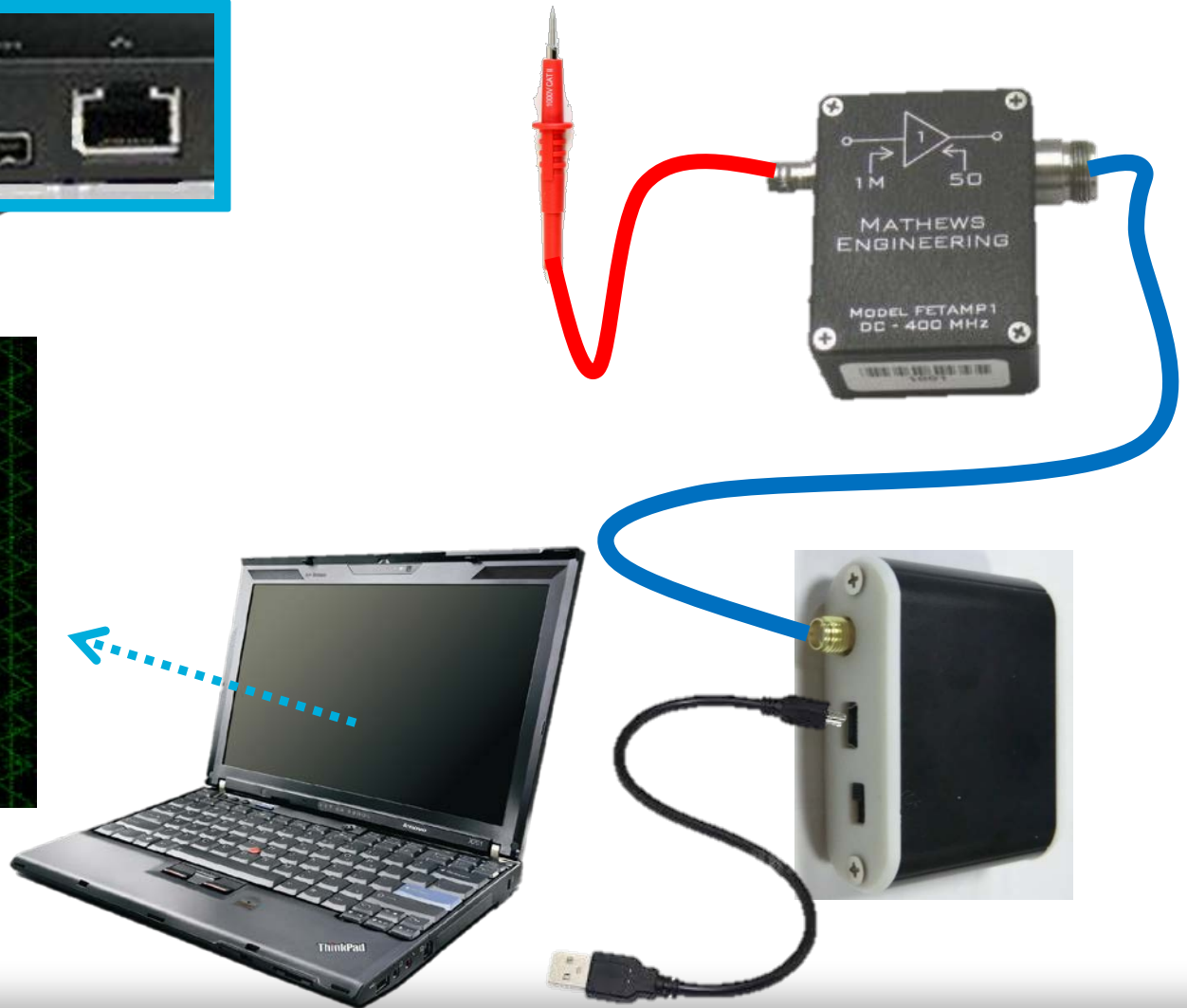
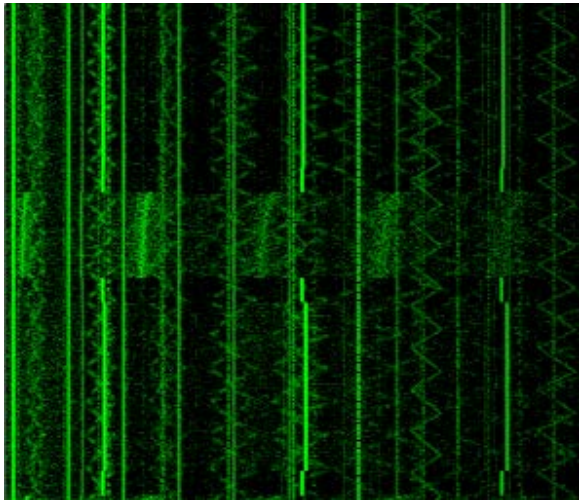
*affects* currents and EM fields  
*dumped to* device ground  
*connected to* conductive chassis

Key = ← .....  
101011...




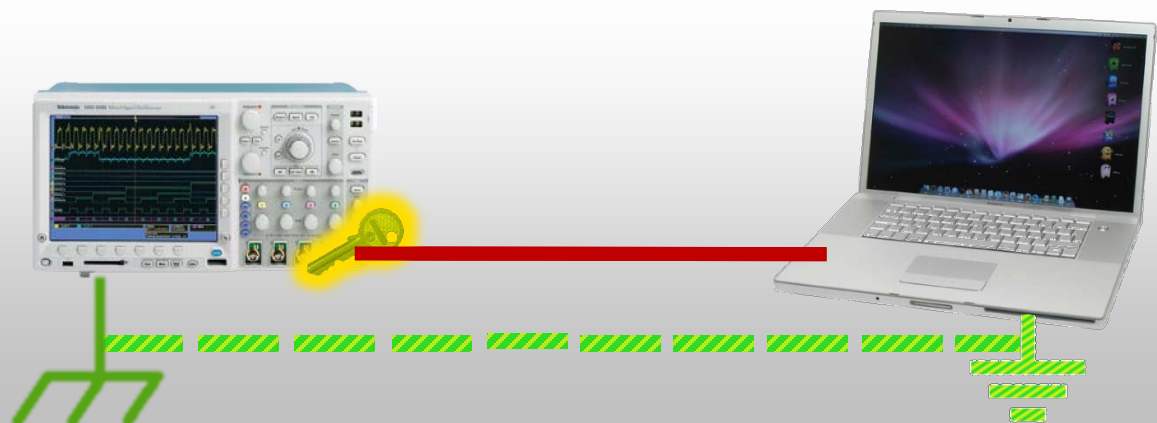


# Connecting to the chassis

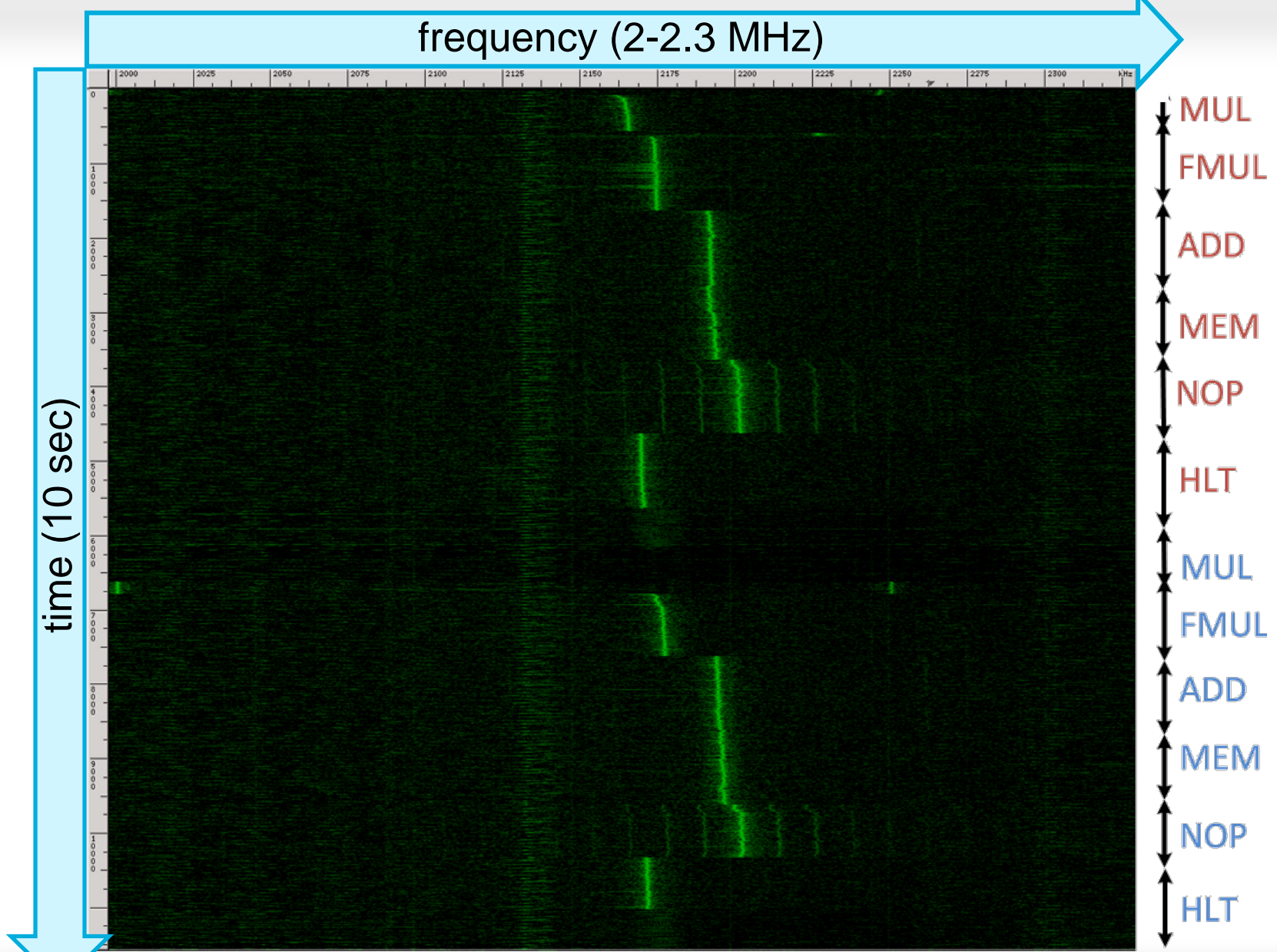


# Demo: distinguishing instructions

Key =   
101011...



# Distinguishing various CPU operations



# Low-bandwidth leakage of RSA

# Definitions (RSA)

## Key setup

- **sk:** random primes  $p, q$ , private exponent  $d$
- **pk:**  $n = pq$ , public exponent  $e$

## Encryption

$$c = m^e \bmod n$$

## Decryption

$$m = c^d \bmod n$$

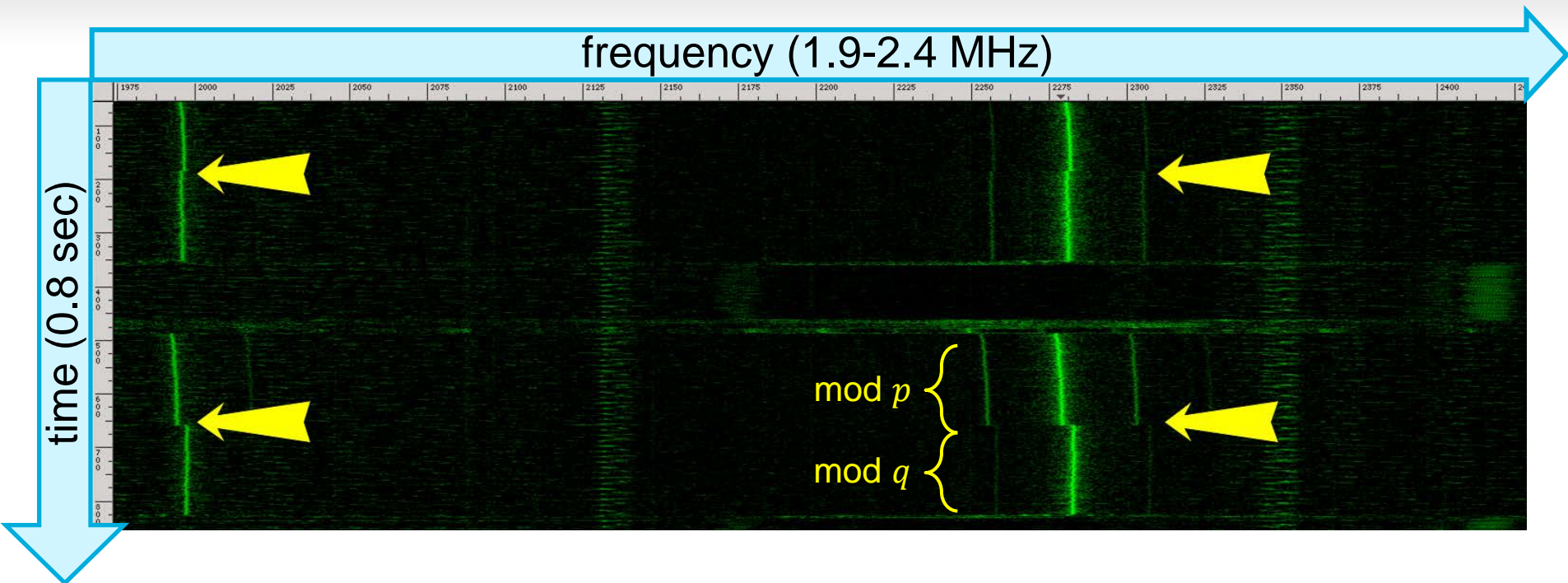
A quicker way used by most implementations

$$m_p = c^{d_p} \bmod p$$

$$m_q = c^{d_q} \bmod q$$

Obtain  $m$  using Chinese Remainder Theorem

# GnuPG RSA key distinguishability



Can distinguish between:

1. Decryptions and other operations
2. Two exponentiations (mod  $p$ , mod  $q$ )
3. Different keys
4. Different primes

# Key extraction

# GnuPG modular exponentiation

```
modular_exponentiation(c, d, p) {
```

```
  m=1
```

```
  for i=n to 1 do
```

```
    m = m2 mod p
```

```
    t = m*c mod p //always mult
```

```
    if d[i]==1 then
```

```
      m=t
```

```
  return m
```

$$m = c^{d_n \cdots d_{i+1}} \bmod p$$

$$m = c^{d_n \cdots d_{i+1} 0} \bmod p$$

$$t = c^{d_n \cdots d_{i+1} 1} \bmod p$$

$$m = c^{d_n \cdots d_i} \bmod p$$

Q: Why always **compute**  $t \leftarrow m \cdot c$  then **conditionally copy**?

A: This is a side channel countermeasure meant to protect  $d$

no key dependent  
operation to measure



```
}
```



# GnuPG modular exponentiation

```
modular_exponentiation(c,d,p) {  
  m=1  
  for i=n to 1 do  
    m = m2 mod p  
    t = m*c mod p //always mult  
    if d[i]==1 then  
      m=t  
  return m  
}
```

*m* depends on both *d[i]* and *c*

*m* is squared in next iteration of the main loop

2GHz CPU speed vs. 1.5MHz measurements  
can only see drastic changes inside squaring operation



craft *c* to affect the squaring in the next loop iteration, based on *d[i]*

measure changes inside squaring operation and obtain *d[i]*

**Idea: leakage self-amplification**  
abuse algorithm's own code to amplify its own leakage!

1. Craft suitable cipher-text to affect the inner-most loop
2. Small differences in repeated inner-most loops cause a big overall difference in code behavior

# Non-adaptive key extraction (similar to [Yen, Lien, Moon and Ha 05])

```
modular_exponentiation(c, d, p) {
```

$m = 1$

for  $i = n$  to 1 do

$m = m^2 \bmod p$

$t = m * c \bmod p$  //always mult

if  $d[i] == 1$

$m \equiv \pm 1$   
 $m = t$

return  $m$

```
karatsuba_sqr( m ) {
```

```
... 0/$
basic_sqr( x )
```

```
basic_sqr( x )
```

```
...
if( x[j] == 0 )
    y = 0
else
    y = x[j] * x
```

$c \equiv -1 \pmod{p}$

$m \equiv 1 \pmod{p}$

$t \equiv -1 \pmod{p}$

Many zeros or random looking, based on  $d[i]$

If  $d[i] == 1$  then  $m \equiv -1 \pmod{p}$  so bits of  $m$  are "random".

If  $d[i] == 0$  then  $m \equiv 1 \pmod{p}$  so bits of  $m$  have many zeros.

repeated 189 times per bit of  $d$

~0.2ms of measurement per bit of  $d$

# A chosen ciphertext attack

Non-adaptive ciphertext choice  $c \equiv -1 \pmod{p}$   
(similar to [YLMH05]):

- RSA:  $c = N - 1$
- ElGamal:  $c = p - 1$

Overall attack performance:

Algorithm	Attack type	# ciphertexts	Time	BW	Cipher	Ref
Sqr-and-always-mlt	Non-adaptive chosen ciphertext	1	3 sec	2 MHz	ElGamal, RSA	[GPT14]

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Non-adaptive ciphertext choice  $c \equiv -1 \pmod{p}$   
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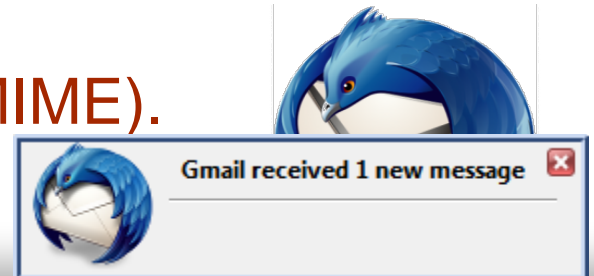
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- ElGamal:  $c = p - 1$

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## Ciphertext injection

Send chosen ciphertexts via email (PGP/MIME).  
Decrypted by email client (e.g., Enigmail) automatically.

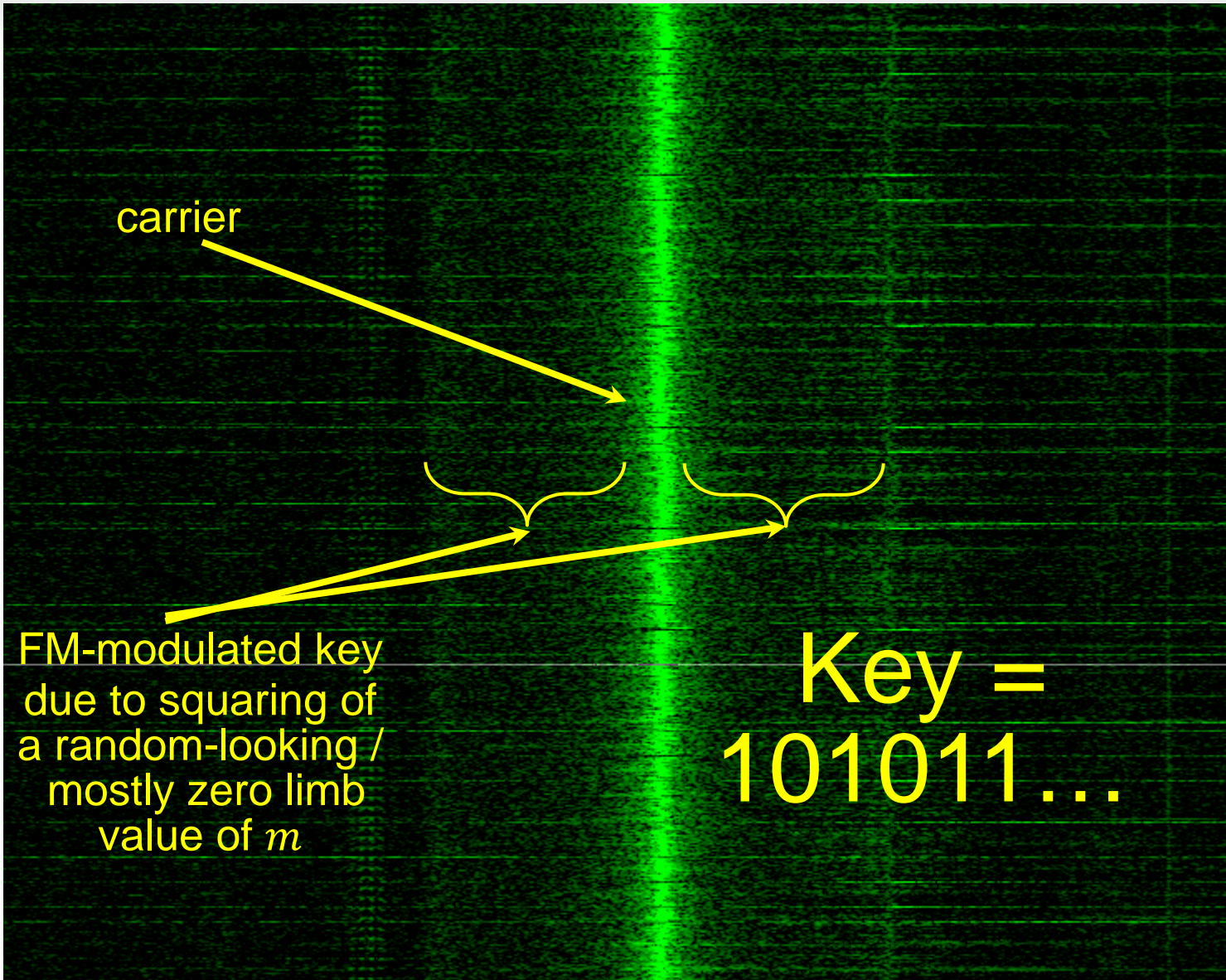


**Empirical results:  
ground-potential attacks**

Demo:  
RSA key extraction  
from chassis potential



# Reading the secret key (non-adaptive attack)



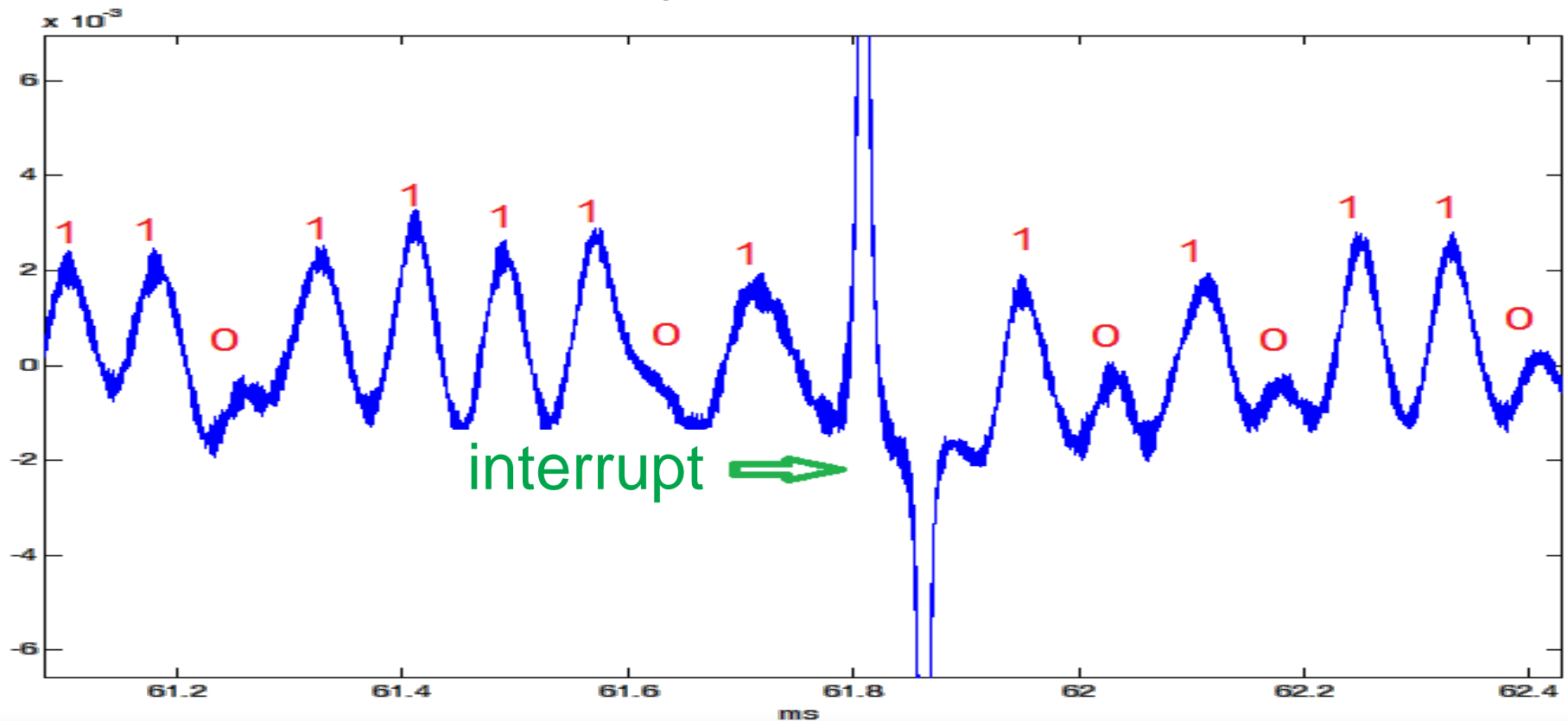
carrier

FM-modulated key  
due to squaring of  
a random-looking /  
mostly zero limb  
value of  $m$

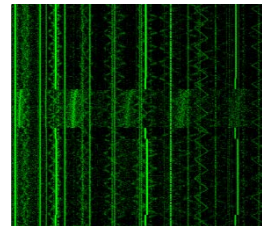
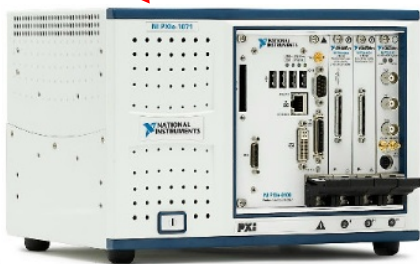
Key =  
101011...

# Reading the secret key (non-adaptive attack)

- Acquire trace
- Filter around carrier (1.7 MHz)
- FM demodulation
- Read out bits (“simple ground analysis”)



# RSA and ElGamal key extraction in a few seconds using human touch (non-adaptive attack)



Key =  
101011...

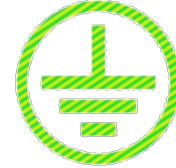
# Ground-potential analysis

- **Attenuating EMI emanations**

“Unwanted currents or electromagnetic fields?

Dump them to the circuit ground!”

(Bypass capacitors, RF shields, ...)



- Device is grounded, but its “ground” potential fluctuates relative to the mains earth ground.



Computation

*affects*

currents and EM fields

*dumped to*

device ground

*connected to*

conductive chassis



# Ground-potential analysis

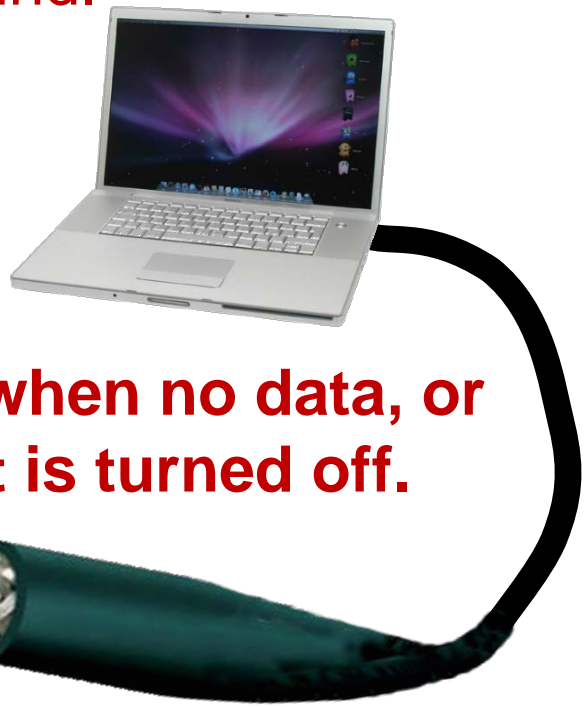
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“Unwanted currents or electromagnetic fields?  
Dump them to the circuit ground!”  
(Bypass capacitors, RF shields, ...)
- Device is grounded, but its “ground” potential fluctuates relative to the mains earth ground.



## Computation

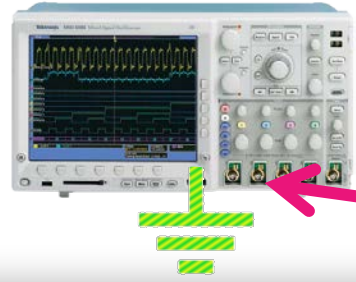
*affects*  
*dumped to*  
*connected to*  
*connected to*

currents and EM fields  
device ground  
conductive chassis  
shielded cables



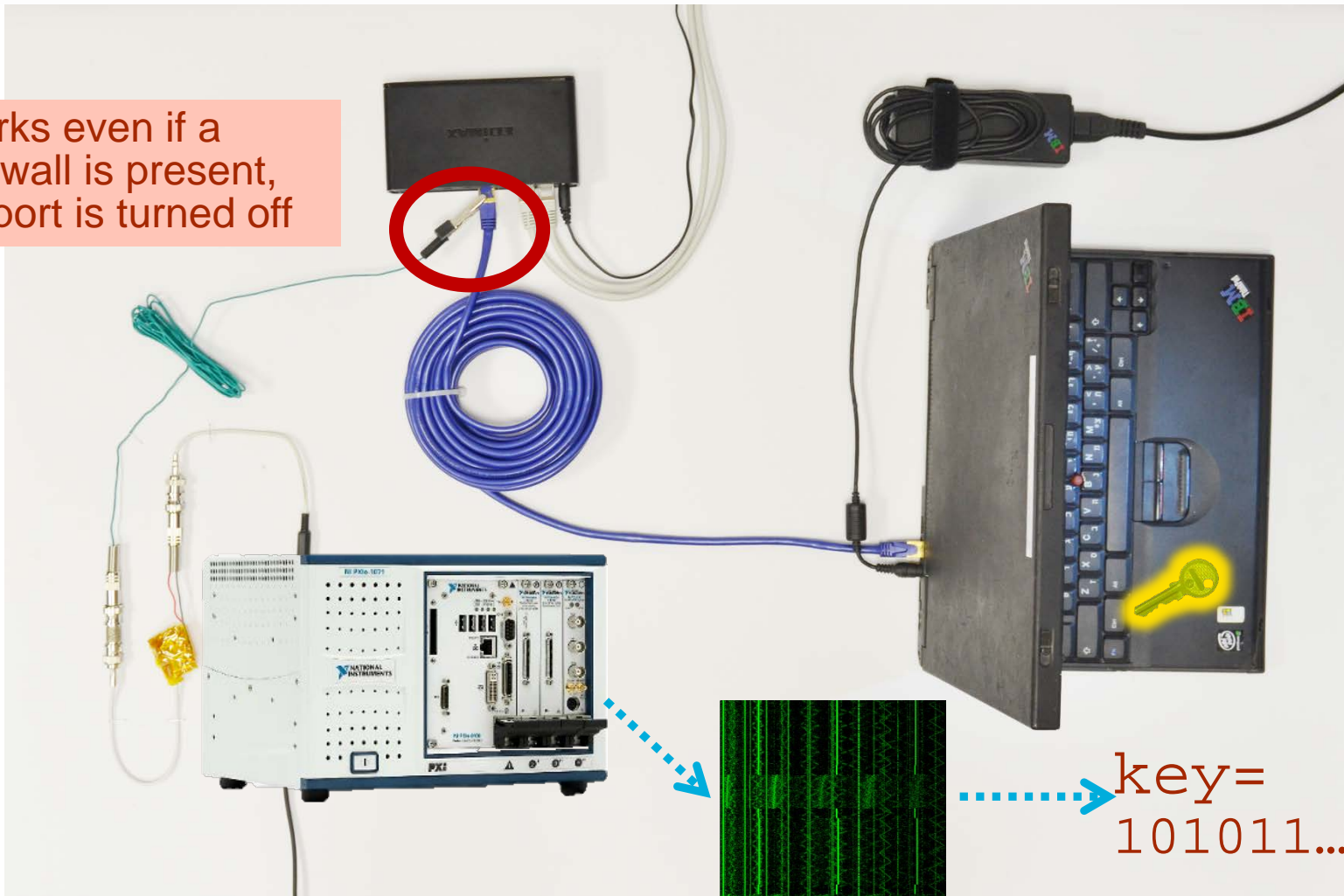
**Even when no data, or port is turned off.**

Key = ←...  
101011...



# RSA and ElGamal key extraction in a few seconds using the far end of 10 meter network cable

works even if a  
firewall is present,  
or port is turned off



# Empirical results: electromagnetic attacks

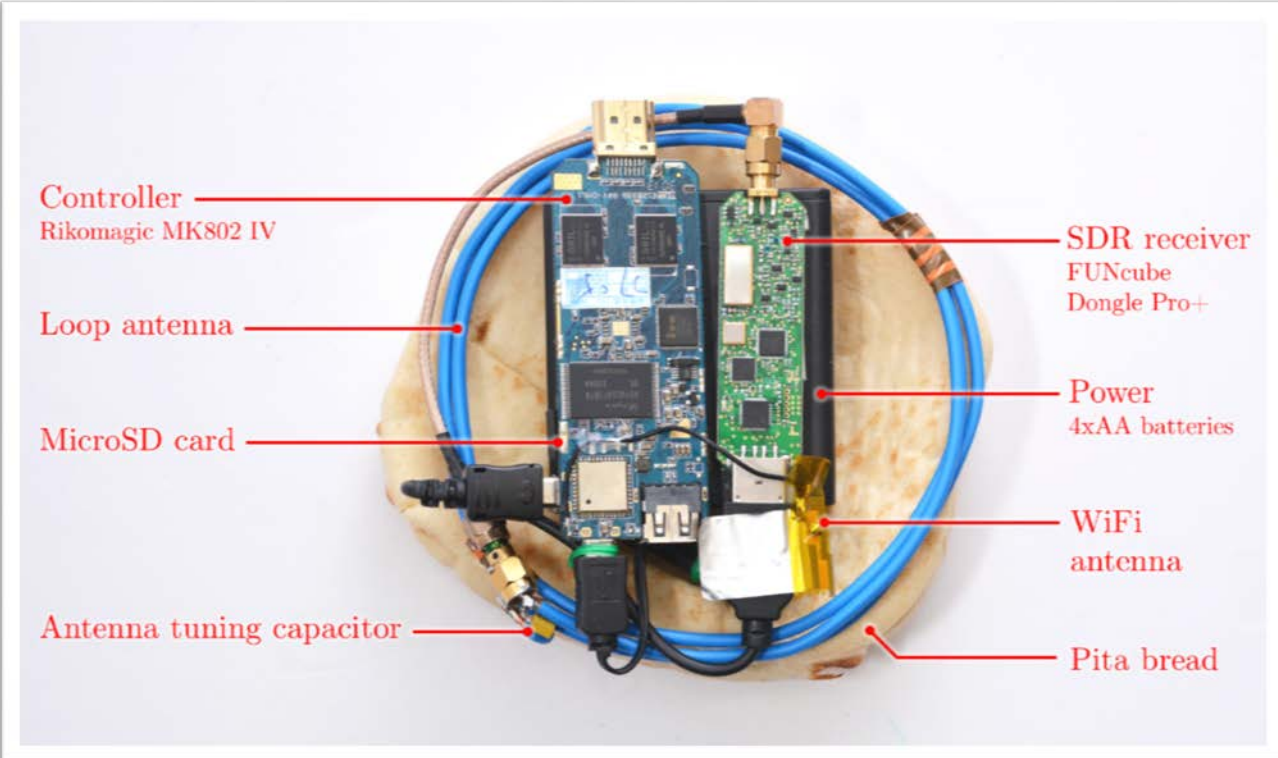
# Electromagnetic key extraction

- Currents inside the target create electromagnetic waves.
- Can be detected using an electromagnetic probe (e.g., a loop of cable).





# Portable Instrument for Trace Acquisition



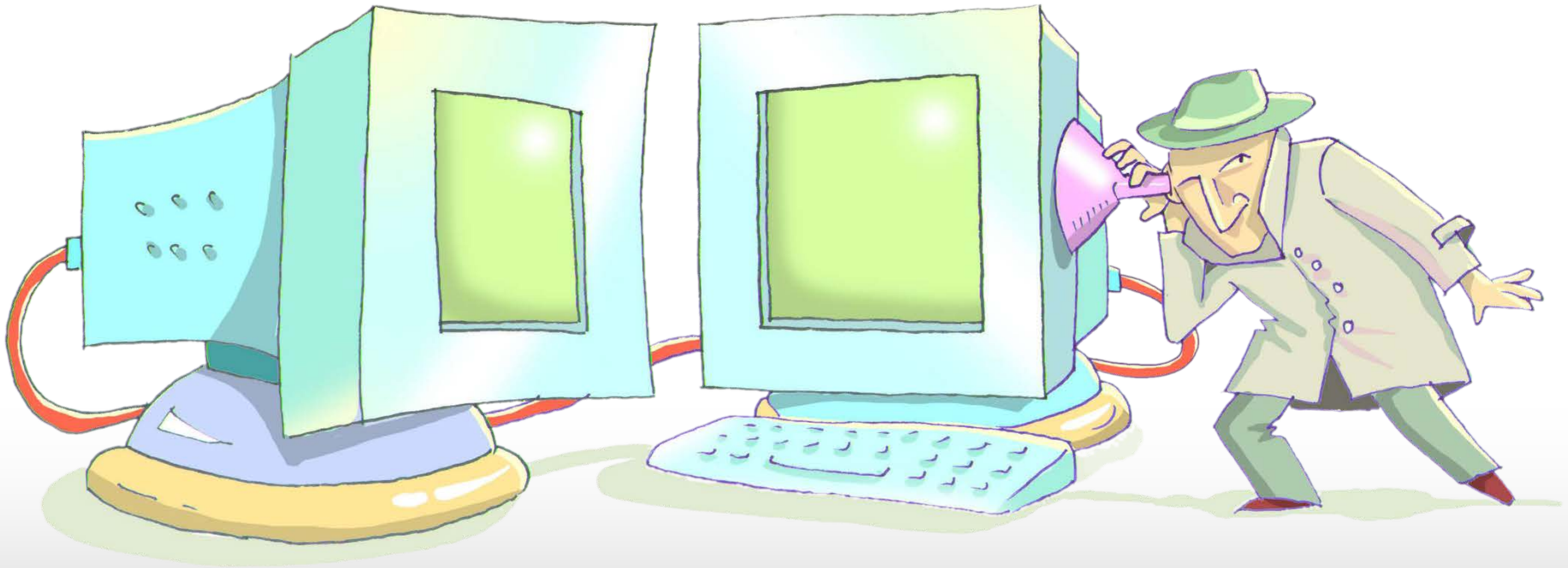
Cost to build: ~300\$



# Key extraction via commodity radio receiver



# Acoustic cryptanalysis



# Acoustic emanations from PCs

- Noisy electrical components in the voltage regulator



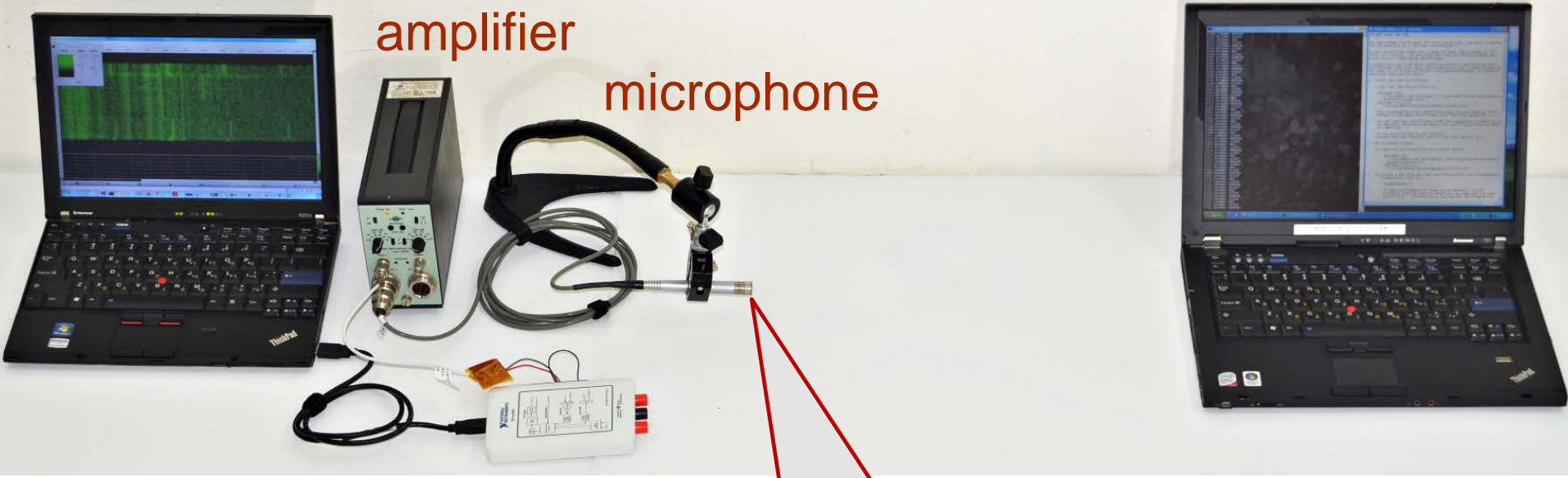
Bzzzzzz

- Commonly known as “coil-whine” but also originates from capacitors

# Experimental setup (example)

attacker

target



amplifier

microphone

digitizer



# Adaptive key extraction

Severe attenuation of high frequency signals.

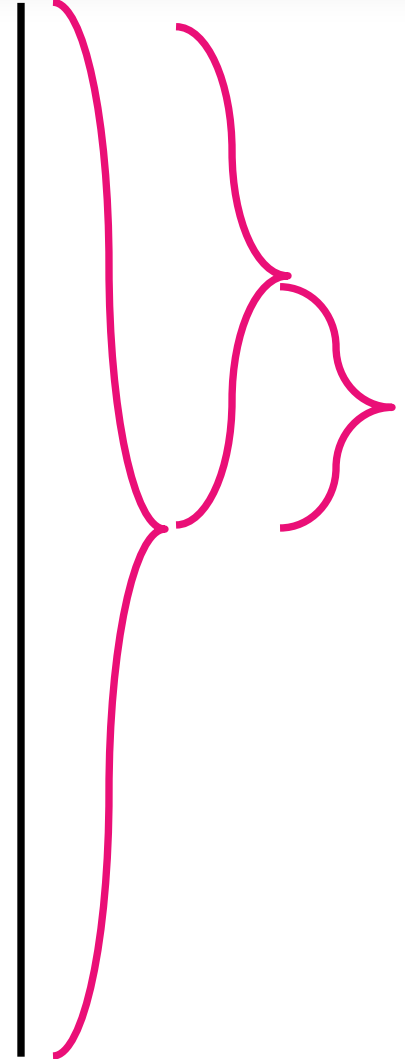
- Effective bandwidth of 50 kHz
- Cannot observe a single squaring

Make the entire decryption depend on a single attacked bit

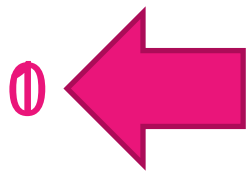
- Extreme version of self-amplification
- Extract the prime  $q$  bit-by-bit (adaptive chosen ciphertext)
- Total #measurements:  
2048 decryptions for RSA-4096 (~1 hour)

# An adaptive chosen-ciphertext attack

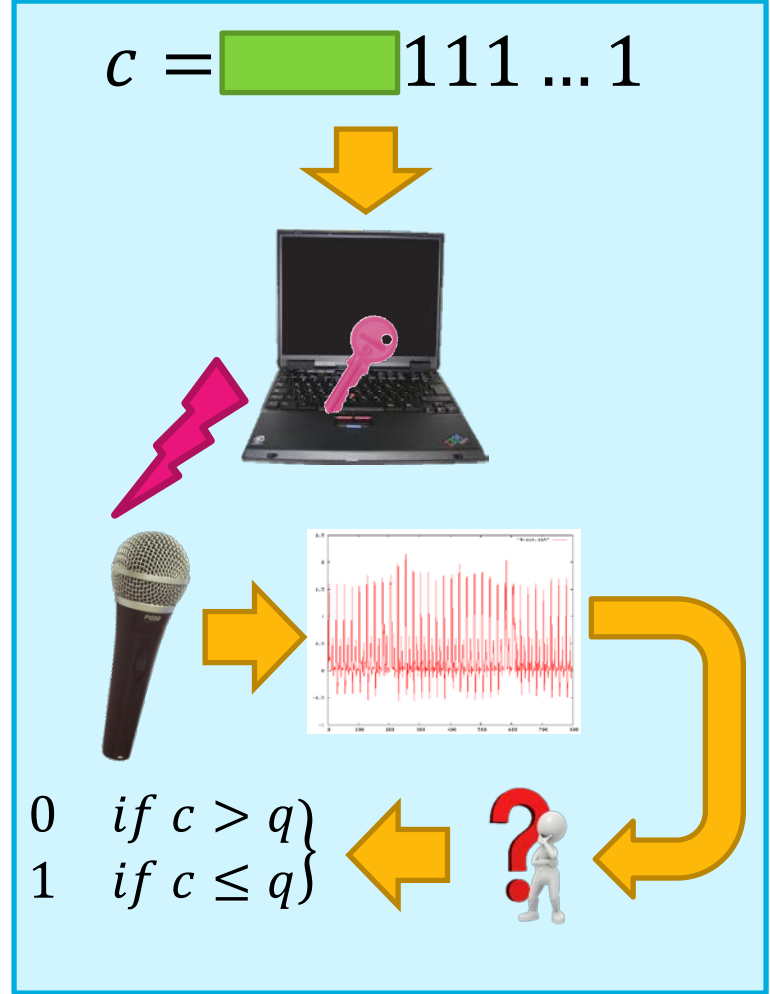
1111...1



- $q = 11?????? \dots$
- $q = 11011010 \dots$
- $q = 110????? \dots$
- $q = 1??????? \dots$
- $c = 10111111\dots$



## Bit-distinguisher oracle



# An adaptive chosen-ciphertext attack

Total #measurements:

$$\frac{\text{Key size}}{2 \cdot 2} \cdot 2$$

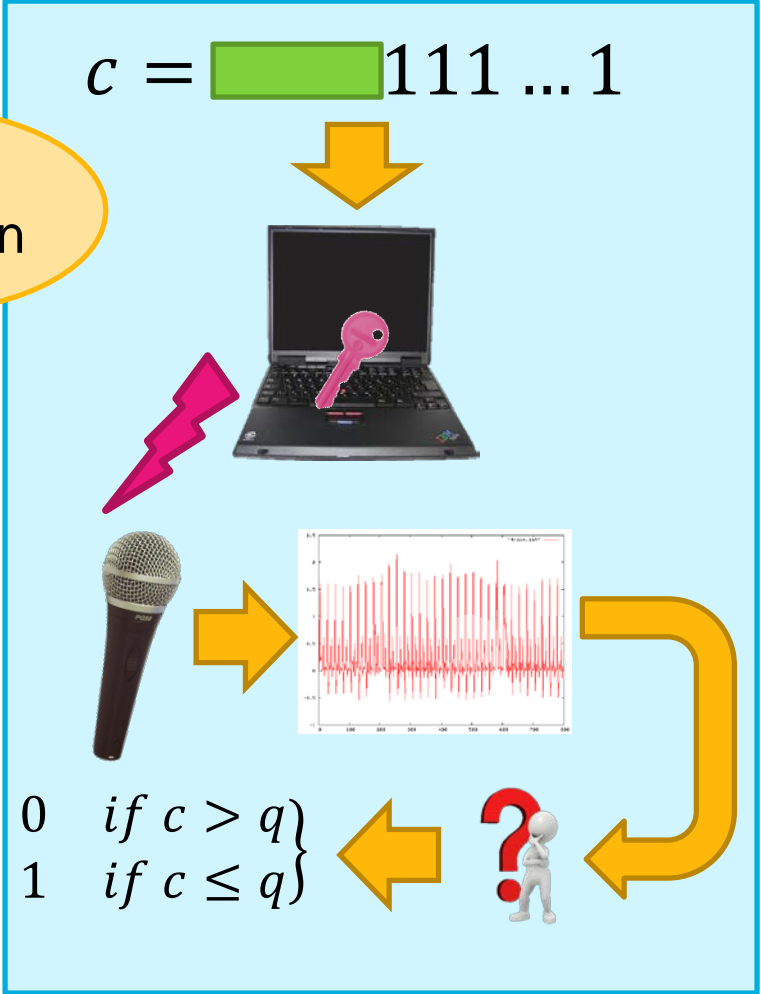
Just  $q$

Coppersmith lattice reduction:  
half the bits suffice

Error correction

Overall: 2048 decryptions for RSA-4096 (~1 hour)

## Bit distinguisher oracle





# GnuPG RSA decryption - $m_q = c^{d_q} \text{ mod } q$

```
modular_exponentiation(c, d, q) {  
  ...  
  karatsuba_mult(m, c)  
  ...  
  karatsuba_mult(m, c) {  
    ...  
    basic_mult(x, y)  
    ...  
    basic_mult(x, y) {  
      ...  
      if (y[j] == 0) x7  
        return 0  
      else  
        return y[j] * x  
    }  
  }  
}
```

Grand total:  
272384 times  
~0.5 sec of  
measurements

x2048  
x19  
craft c such that  
 $q_i = 1 \rightarrow y[j] = 0$   
 $q_i = 0 \rightarrow y[j] \neq 0$   
(for most j's)

# Extracting $q_i$ (simplified)

GnuPG's modular exponentiation (see function `mpi_powm` in `mpi/mpi-pow.c`).

**Input:** Three integers  $c$ ,  $d$  and  $q$  in binary representation such that  $d = d_n \cdots d_1$ .

**Output:**  $m = c^d \pmod q$ .

```

1: procedure MODULAR_EXPONENTIATION( $c, d, q$ )
2:   if SIZE_IN_LIMBS( $c$ ) > SIZE_IN_LIMBS( $q$ ) then
3:      $c \leftarrow c \pmod q$ 
4:    $m \leftarrow 1$ 
5:   for  $i \leftarrow n$  downto 1 do
6:      $m \leftarrow m^2$ 
7:     if SIZE_IN_LIMBS( $m$ ) > SIZE_IN_LIMBS( $q$ ) then
8:        $m \leftarrow m \pmod q$ 
9:     if SIZE_IN_LIMBS( $c$ ) < KARATSUBA_THRESHOLD then
10:       $t \leftarrow \text{MUL\_BASECASE}(m, c)$ 
11:    else
12:       $t \leftarrow \text{MUL}(m, c)$ 
13:    if SIZE_IN_LIMBS( $t$ ) > SIZE_IN_LIMBS( $q$ ) then
14:       $t \leftarrow t \pmod q$ 
15:    if  $d_i = 1$  then
16:       $m \leftarrow t$ 
17:   return  $m$ 
18: end procedure
  
```

$c^i = q_{2048} \cdots q_{i+1} 01 \cdots 1$

If  $q_i = 1$  then  $c^i < q$ , thus  $c = c^i$ . That is,  $c$  has special structure.

If  $q_i = 0$  then  $2q > c^i > q$ , thus  $c = c^i - q$ . That is,  $c$  is random looking.

and we now multiply by  $c$  causing the bit-dependent leakage.

# Extracting $q_i$

GnuPG's modular exponentiation (see function `mpi_powm` in `mpi/mpi-pow.c`).

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```

$c^i = q_{2048} \cdots q_{i+1} 01 \cdots 1 + n$

If  $q_i = 1$  then  $c^i - n < q$ , thus  $c = c^i - n$ . That is,  $c$  has special structure.

If  $q_i = 0$  then  $2q > c^i - n > q$ , thus  $c = c^i - q - n$ . That is,  $c$  is random looking.

and we now multiply by  $c$  causing the bit-dependent leakage.

# Extracting $q_i$ (problem)

GnuPG's modular exponentiation (see function `mpi_powm` in `mpi/mpi-pow.c`).

**Input:** Three integers  $c$ ,  $d$  and  $q$  in binary representation such that  $d = d_n \cdots d_1$ .

**Output:**  $m = c^d \pmod q$ .

```
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18: end procedure
```

▷ defined as 16  
▷ Compute  $t \leftarrow m \cdot c$   
▷ Compute  $t \leftarrow m \cdot c$



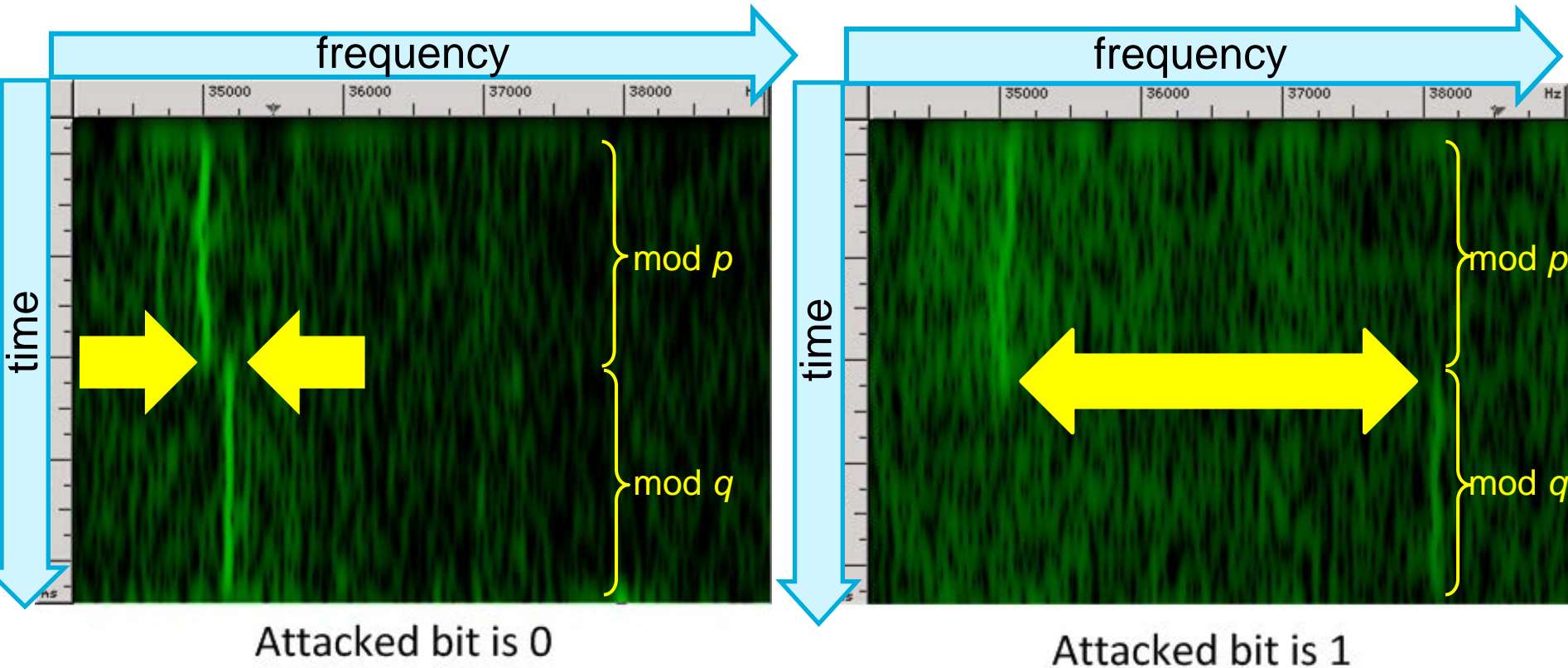
Multiplication is repeated  
2048 times (0.5 sec of data)



Single multiplication is way  
too fast for us to measure

# Empirical results: acoustic attacks

# Distinguishing a key bit by a spectral signature



# Demo: key extraction

# Acoustic: results

RSA 4096-bit key extraction from 1 meter away using a microphone





# Acoustic: results

RSA 4096-bit key extraction from  
**10 meters** away using a parabolic microphone



# Acoustic: results

RSA 4096-bit key extraction from 30cm away using a smartphone



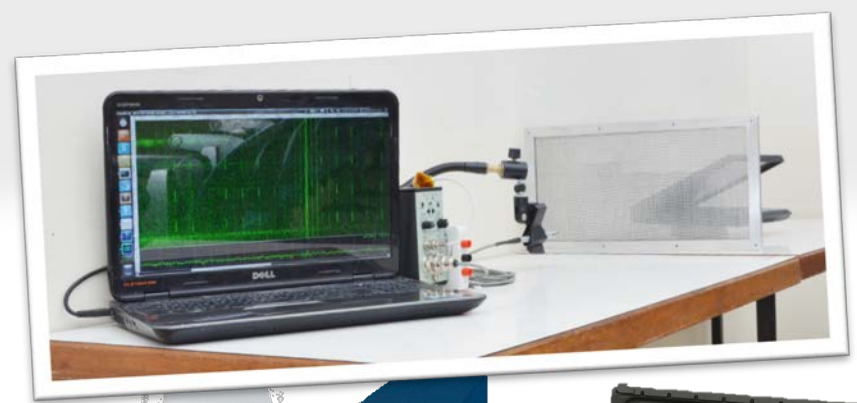
# Countermeasures

# Countermeasures

## Common suggestions

### 1. Shielding

- EM (Faraday cages), ground  
*difficult and expensive*
- Acoustic? *Vents!*



### 2. Add analog noise (*expensive, correlations remain*)

### 3. Parallel software load (*inadequate, may help attacker*)

*Attacks rely on decryption of chosen ciphertexts.*

*Solution: ciphertext randomization use equivalent but random-looking ciphertexts*

- *Negligible slowdown for RSA*
- *x2 slowdown for ElGamal*



Effective countermeasure:  
ciphertext randomization (added in GnuPG 1.4.16)

Given a ciphertext  $c$ :

1. Generate a random number  $r$  and compute  $r^e$
2. Decrypt  $r^e \cdot c$  and obtain  $m'$
3. Output  $m' \cdot r^{-1}$

Works since  $ed = 1 \text{ mod } \varphi(n)$  thus:

$$\begin{aligned}(r^e \cdot c)^d \cdot r^{-1} \text{ mod } n &= r^{ed} \cdot r^{-1} \cdot c^d \text{ mod } n \\ &= r \cdot r^{-1} \cdot c^d \text{ mod } n \\ &= c^d \text{ mod } n \\ &= m\end{aligned}$$

[tau.ac.il/~tromer/acoustic](http://tau.ac.il/~tromer/acoustic)

CRYPTO'14

CVE 2013-4576

[tau.ac.il/~tromer/handsoff](http://tau.ac.il/~tromer/handsoff)

CHES'14

CVE-2014-5270

[tau.ac.il/~tromer/radioexp](http://tau.ac.il/~tromer/radioexp)

CHES'15

CVE-2014-3591

